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 10/02/88 36 U.S. PTO	UTILITY PATENT APPLICATION TRANSMITTAL (Small Entity) (Only for new nonprovisional applications under 37 CFR 1.53(b))	Docket No. 0205/US
		Total Pages in this Submission 103

TO THE ASSISTANT COMMISSIONER FOR PATENTS
 Box Patent Application
 Washington, D.C. 20231

Transmitted herewith for filing under 35 U.S.C. 111(a) and 37 C.F.R. 1.53(b) is a new utility patent application for an invention entitled:

AUTOMATED OPTICAL MEASUREMENT APPARATUS AND METHOD

and invented by:

Stephen D. Fantone, Stephen Wilk, Jian Zhang, and Daniel J. Braunstein

 36 U.S. PTO
 09/67679
 10/02/88

 If a **CONTINUATION APPLICATION**, check appropriate box and supply the requisite information:

☐ Continuation ☐ Divisional ☒ Continuation-in-part (CIP) of prior application No.: 09/328,972

Which is a:

☐ Continuation ☐ Divisional ☐ Continuation-in-part (CIP) of prior application No.:

Which is a:

☐ Continuation ☐ Divisional ☐ Continuation-in-part (CIP) of prior application No.:

Enclosed are:

Application Elements

1. ☒ Filing fee as calculated and transmitted as described below
2. ☒ Specification having 44 pages and including the following:
 - a. ☒ Descriptive Title of the Invention
 - b. ☒ Cross References to Related Applications (if applicable)
 - c. ☐ Statement Regarding Federally-sponsored Research/Development (if applicable)
 - d. ☐ Reference to Microfiche Appendix (if applicable)
 - e. ☒ Background of the Invention
 - f. ☒ Brief Summary of the Invention
 - g. ☒ Brief Description of the Drawings (if drawings filed)
 - h. ☒ Detailed Description
 - i. ☒ Claim(s) as Classified Below
 - j. ☒ Abstract of the Disclosure

UTILITY PATENT APPLICATION TRANSMITTAL
(Small Entity)

(Only for new nonprovisional applications under 37 CFR 1.53(b))

Docket No.
0205/US

Total Pages in this Submission
103

Application Elements (Continued)

3. ☒ Drawing(s) *(when necessary as prescribed by 35 USC 113)*
- a. ☒ Formal b. ☐ Informal Number of Sheets 22
4. ☒ Oath or Declaration
- a. ☒ Newly executed *(original or copy)* ☐ Unexecuted
- b. ☐ Copy from a prior application (37 CFR 1.63(d)) *(for continuation/divisional application only)*
- c. ☒ With Power of Attorney ☐ Without Power of Attorney
- d. ☐ DELETION OF INVENTOR(S)
Signed statement attached deleting inventor(s) named in the prior application,
see 37 C.F.R. 1.63(d)(2) and 1.33(b).
5. ☐ Incorporation By Reference *(usable if Box 4b is checked)*
The entire disclosure of the prior application, from which a copy of the oath or declaration is supplied under
Box 4b, is considered as being part of the disclosure of the accompanying application and is hereby
incorporated by reference therein.
6. ☐ Computer Program in Microfiche
7. ☐ Genetic Sequence Submission *(if applicable, all must be included)*
- a. ☐ Paper Copy
- b. ☐ Computer Readable Copy
- c. ☐ Statement Verifying Identical Paper and Computer Readable Copy

Accompanying Application Parts

8. ☒ Assignment Papers *(cover sheet & documents)*
9. ☐ 37 CFR 3.73(b) Statement *(when there is an assignee)*
10. ☐ English Translation Document *(if applicable)*
11. ☐ Information Disclosure Statement/PTO-1449 ☐ Copies of IDS Citations
12. ☐ Preliminary Amendment
13. ☒ Acknowledgment postcard
14. ☒ Certificate of Mailing
- ☐ First Class ☒ Express Mail *(Specify Label No.):* EL392197993US

UTILITY PATENT APPLICATION TRANSMITTAL (Small Entity)

(Only for new nonprovisional applications under 37 CFR 1.53(b))

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103

Accompanying Application Parts (Continued)

15. ☐ Certified Copy of Priority Document(s) (if foreign priority is claimed)
16. ☒ Small Entity Statement(s) - Specify Number of Statements Submitted: ONE (1)
17. ☒ Additional Enclosures (please identify below):

Second set of formal drawings consisting of 22 sheets and a copy of this sheet

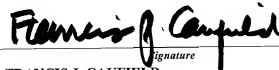
Fee Calculation and Transmittal

CLAIMS AS FILED

For	#Filed	#Allowed	#Extra	Rate	Fee
Total Claims	25	- 20 =	5	x \$9.00	\$45.00
Indep. Claims	3	- 3 =	0	x \$39.00	\$0.00
Multiple Dependent Claims (check if applicable) <input type="checkbox"/>					\$0.00
BASIC FEE					\$345.00
OTHER FEE (specify purpose) <u>Assignment Recordal Fee</u>					\$40.00
TOTAL FILING FEE					\$430.00

- ☒ A check in the amount of **\$430.00** to cover the filing fee is enclosed. Check No. **005137**
- ☒ The Commissioner is hereby authorized to charge and credit Deposit Account No. **03-1150** as described below. A duplicate copy of this sheet is enclosed.
- ☐ Charge the amount of _____ as filing fee.
- ☒ Credit any overpayment.
- ☒ Charge any additional filing fees required under 37 C.F.R. 1.16 and 1.17.
- ☐ Charge the issue fee set in 37 C.F.R. 1.18 at the mailing of the Notice of Allowance, pursuant to 37 C.F.R. 1.311(b).

Dated: OCT. 2, 2000


signature

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CC:

**VERIFIED STATEMENT (DECLARATION) CLAIMING SMALL ENTITY
STATUS (37 CFR 1.9(f) AND 1.27 (c)) - SMALL BUSINESS CONCERN**

Docket No.
0205/US

Serial No.

Filing Date

Patent No.

Issue Date

filed concurrently herewith

Applicant/ Patentee: **Stephen D. Fantone, Stephen Wilk, Jian Zhang, and Daniel J. Braunstein**

Invention:

AUTOMATED OPTICAL MEASUREMENT APPARATUS AND METHOD

I hereby declare that I am:

- ☐ the owner of the small business concern identified below:
- ☒ an official of the small business concern empowered to act on behalf of the concern identified below:

NAME OF CONCERN: **OPTIKOS CORPORATION**ADDRESS OF CONCERN: **286 Cardinal Medeiros Avenue, Cambridge, MA 02141**

I hereby declare that the above-identified small business concern qualifies as a small business concern as defined in 13 CFR 121.3-18, and reproduced in 37 CFR 1.9(d), for purposes of paying reduced fees under Section 41(a) and (b) of Title 35, United States Code, in that the number of employees of the concern, including those of its affiliates, does not exceed 500 persons. For purposes of this statement, (1) the number of employees of the business concern is the average over the previous fiscal year of the concern of the persons employed on a full-time, part-time or temporary basis during each of the pay periods of the fiscal year, and (2) concerns are affiliates of each other when either, directly or indirectly, one concern controls or has the power to control the other, or a third party or parties controls or has the power to control both.

I hereby declare that rights under contract or law have been conveyed to and remain with the small business concern identified above with regard to the above identified invention described in:

- ☒ the specification filed herewith with title as listed above.
- ☐ the application identified above.
- ☐ the patent identified above.

If the rights held by the above-identified small business concern are not exclusive, each individual, concern or organization having rights to the invention is listed on the next page and no rights to the invention are held by any person, other than the inventor, who could not qualify as an independent inventor under 37 CFR 1.9(c) or by any concern which would not qualify as a small business concern under 37 CFR 1.9(d) or a nonprofit organization under 37 CFR 1.9(e).

Each person, concern or organization to which I have assigned, granted, conveyed, or licensed or am under an obligation under contract or law to assign, grant, convey, or license any rights in the invention is listed below:

- ☒ no such person, concern or organization exists.
☐ each such person, concern or organization is listed below.

FULL NAME **NONE**

ADDRESS

☐ Individual ☐ Small Business Concern ☐ Nonprofit Organization

FULL NAME

ADDRESS

☐ Individual ☐ Small Business Concern ☐ Nonprofit Organization

FULL NAME

ADDRESS

☐ Individual ☐ Small Business Concern ☐ Nonprofit Organization

FULL NAME

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☐ Individual ☐ Small Business Concern ☐ Nonprofit Organization

Separate verified statements are required from each named person, concern or organization having rights to the invention averring to their status as small entities. (37 CFR 1.27)

I acknowledge the duty to file, in this application or patent, notification of any change in status resulting in loss of entitlement to small entity status prior to paying, or at the time of paying, the earliest of the issue fee or any maintenance fee due after the date on which status as a small entity is no longer appropriate. (37 CFR 1.28(b))

I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under Section 1001 of Title 18 of the United States Code, and that such willful false statements may jeopardize the validity of the application, any patent issuing thereon, or any patent to which this verified statement is directed.

NAME OF PERSON SIGNING:

Stephen D. Fantone

TITLE OF PERSON SIGNING

OTHER THAN OWNER:

President

ADDRESS OF PERSON SIGNING:

OPTIKOS CORPORATION

286 Cardinal Medeiros Avenue

Cambridge, MA 02141

SIGNATURE:



DATE:

9/23/00

IN THE UNITED STATES PATENT AND TRADEMARK OFFICE

PATENT APPLICATION OF

STEPHEN D. FANTONE, STEPHEN WILK, JIAN ZHANG, AND
DANIEL J. BRAUNSTEIN

FOR

AUTOMATED OPTICAL MEASUREMENT APPARATUS AND METHOD

"EXPRESS MAIL" mailing label number EL392197993US

Date of Deposit: October 2, 2000

I hereby certify that this application is being deposited with the U.S. Postal Service "Express Mail Post Office to Addressee" service under 37 CFR 1.10 on the date indicated above and is addressed to BOX PATENT APPLICATION, Assistant Commissioner For Patents, Washington, D.C. 20231


Francis J. Caufield
Registration No. 27,425

**TITLE: AUTOMATED OPTICAL MEASUREMENT APPARATUS
AND METHOD**

CROSS REFERENCE TO RELATED APPLICATION

This application is a Continuation-In-Part of United States Patent Application No. 09/328,972 filed on June 9, 1999 and also claims priority from United States Provisional Patent Application No. 60/160,949 filed on October 22, 1999, both of which are incorporated by reference herein in their entirety.

BACKGROUND OF THE INVENTION

This invention generally relates to methods and apparatus for testing optical systems and particularly to devices and techniques for the automated measurement of a variety of parameters of optical surfaces and/or elements including radii of curvature, surface shape, thickness, power, focal length, wavefront, topography, and aberrations.

Throughout the process for fabricating optical systems or components, it is frequently necessary to determine if, and how well, optical surfaces or elements conform to their designers stated requirements. Not only does the performance of optical systems in final form need to be verified, but various parameters of their components need to undergo intermediate testing for conformance with their specifications prior to final assembly as a system. Indeed, even the tools of fabrication, especially molds for the formation of plastic or glass lens elements, need to be tested for compliance with design specifications. Some of the most frequently encountered measurements that need to be made are radius of curvature of surfaces in either convex or concave form, surface topography, thickness, power, and various focal lengths.

Classically, radius of curvature is measured through the use of a hand-held instrument called a spherometer, which measures the sagittal height (sag) of the surface over a known diameter and then displays the radius of curvature on a dial or other visual display after an internal calculation that relates radius to sag height and the known diameter. However, the accuracy of such devices are prone to relatively large errors because sag heights are usually small dimensions that are difficult to accurately measure mechanically.

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A more accurate technique for radii measurement involves the use of an auto-collimating microscope in an arrangement referred to as a radiuscope. Here, one first focuses on the surface to be measured and then on the center of curvature of the surface where a reticle image has been imaged back on itself by reflection from the test surface. The positions of the microscope are recorded, and the difference between them represents the radius of curvature to limits of accuracy, which depend on the preciseness of the length measurements and the ability of the operator to accurately focus.

Where the spherometer suffers from problems of precision, the use of the radiuscope, which can be accurate to microns if care is taken, is time consuming and dependent on operator skill and experience.

The thickness of an optical element is more or less important depending on its assigned role in a particular design and can be critical where the design relies heavily on its precision for aberration control or the like. Thickness obviously can be measured directly by mechanical means, which may also be automated, but there is always the danger of damaging part surfaces with mechanical approaches.

Power and focal length are always of interest and can be calculated from classical lens makers formulae having knowledge of the various numerical values required as, for example, index of refraction, radii, and thickness.

For rapid qualitative tests other approaches are also often employed. For this purpose, reliance on the Foucault knife-edge test is often made, and while the Foucault test has its uses, it suffers from an inability to sense changes in slope deviation that are changing only slightly in magnitude or direction. For more accurate quantitative results, reliance is made on interferometric and screen methods, such as the Hartmann test, to perform wavefront analysis from which more gross properties may be derived. However, such tests, while informative, have been laborious and time consuming.

While those skilled in the art have provided a variety of ways for measuring many of the foregoing properties of optical elements and systems, there remains a need for an instrument for rapidly and accurately measuring a number of optical properties

virtually simultaneously, and it is a primary object of the present invention to provide such a device.

Another object of the present invention is to provide methods and associated devices for automatically performing wavefront analysis, measuring surface topography, and determining radius of curvature, thickness, power and focal length of optical surfaces and/or elements with minimal dependence on operator skill.

Yet another object of the present invention is to provide an automated instrument for providing statistical analysis of quality in high volume production settings.

Another object of the present invention is to provide apparatus and methods for optically measuring the physical characteristics of surfaces that are at least partially reflective.

Still another object of the present invention is to satisfy all of the foregoing objects with a user-friendly device that is simple in its implementation and low in cost.

Other objects of the invention will in part be obvious and will in part appear hereinafter. A full understanding of the invention will best be had from reading the detailed description to follow in connection with the detailed drawings.

SUMMARY OF THE INVENTION

The invention comprises a system and method for automatically performing dynamic screen testing on a surface and determining its shape from which other optical parameters of interest may be derived and reported. A measuring head, consisting of a source, beamsplitter, objective lens, and lens array with a CCD camera, is mounted on a translation stage and moves along the optic axis of the head relative to the part under test. The part under test is mounted on an appropriate support, such as a three-point support nest, that automatically centers spherical parts on the optical axis of the system.

Light is projected along the optical axis through a microscope objective or other appropriate lens to illuminate the part under test with a predetermined wavefront, preferably spherical, so that subsequent calculations are made simpler if this light is

recollimated parallel to the optical axis of the system. Light reflected from the part under test passes back through the lens, after which it passes through a pellicle or cube beamsplitter towards a CCD camera. A two-dimensional array, preferably in the form of a pair of crossed lenticular screens, is placed in front of the CCD active area so that a series of sharp images are formed on the CCD array. When the system measuring head is positioned so that the focal point of the objective is located near the surface of the part under test or near its center of curvature, then the incoming nearly parallel light produces a series of spots on the CCD active area. The shifts in the pattern of spots are used to determine the shape of the surface under test. Mathematical analysis of this shape provides information on the radius of curvature of the part (if spherical), the "Spherical" and "Cylindrical" radii of curvature of a toric part (along with the angle between the major axes and a given reference axis), and the "Shape Factor" of an aspheric part. For ease of interpretation, the overall shape can be expressed in various ways, including Zernike polynomials. Software performs this analysis and facilitates providing results in many useful forms – contour plots, wire-frame models of deviation, direct readout of coefficients, direct readout of RMS surface form, direct readout of peak-to-valley difference, etc. Display screens are customizable for the engineering specialist or on-the-floor auditing and measurement for production. Custom processing capabilities are available using Visual Basic® and an Object Linking And Embedding (OLE®) interface.

DESCRIPTION OF THE DRAWINGS

The structure and operation of the invention together with other objects and advantages thereof may best be understood by reading the detailed description in connection with the drawings wherein parts have been assigned a unique reference numeral that is used to identify them whenever they appear in a drawing and wherein:

Fig. 1 is a diagrammatic perspective of the automated measuring apparatus of the invention showing an enclosed optical head in combination with a computer workstation;

Fig. 2 is a diagrammatic front perspective view of the optical head of Fig. 1, uncovered so that its major components may be seen;

Fig. 3 is a diagrammatic, right quarter perspective view of the optical head of Fig. 1, uncovered so that its major components may be seen from a different vantage point than that of Fig. 2;

Fig. 4 is a diagrammatic, left quarter perspective view of the optical head of Fig. 1 uncovered so that its major components may be seen from a vantage point different than that of either Fig. 2 or Fig. 3;

Fig. 5 is a diagrammatic elevational view of the major components of the optical head of Fig. 1 showing how a spherical test surface is illuminated with a predetermined wavefront originating at the surface's center of curvature and how that wavefront is reflected from the test surface and subsequently measured;

Fig. 6 is a diagrammatic elevational view of the major components of the optical head of Fig. 1 showing how a spherical test surface is illuminated with a predetermined wavefront focused on the surface and how that wavefront is reflected from the test surface and subsequently measured;

Fig. 7 is a diagrammatic elevational view of the major components of the optical head of Fig. 1 showing how a spherical test surface is illuminated with a predetermined wavefront originating at some location other than the surface's center of curvature and how that wavefront is reflected from the test surface and subsequently measured;

Fig. 8 is a diagrammatic illustration showing the anticipated location of an array of dots from a spherical surface illuminated with a spherical wavefront originating at the surface's center of curvature along with deviations of the dots as the origin of the wavefront passes through the surface's center of curvature (through focus);

Fig. 9 is an enlarged diagrammatic perspective showing how "crossed lenticular" screens are used in the invention to provide an array of equivalent spherical lenses;

Fig. 10 is a screen from a program used in conjunction with the apparatus of the invention to provide a graphical user interface by which properties of a test surface can be displayed, various system instructions issued, and other test unit properties described;

5 Figs. 11A-D are output screens from a computer program used in conjunction with the apparatus to graphically display topographic maps of the surface of a test unit for various states of defocus;

10 Figs. 12A-D are output screens from a computer program used in conjunction with the apparatus of the invention showing various surface contour plots for different states of defocus of a test unit;

Figs. 13 and 14 are output screens illustrating various coefficient plots as a function of the position of a wavefront origin with respect to a test surface for a toric surface and spherical surface, respectively;

Fig. 15 is an output data screen showing measured values for a toric surface;

15 Fig. 16 is a diagrammatic elevational view similar to Fig. 5 with the addition of a lens forward of the microscope objective to enable measurement of long radius parts;

Fig. 17 is a diagrammatic elevational view similar to Fig. 5 except for the absence of the objective which has been removed to enable measurement of flat surfaces that are at least partially reflective;

20 Fig. 18 is a diagrammatic elevational view similar to Fig. 17 except for the presence of an additional mirror and a relay system for measuring the wavefront error of transmissive filters over their bandpass;

Fig. 19 is a diagrammatic elevational view similar to Fig. 17 with the addition of a beam expansion section to measure large flat surfaces;

25 Fig. 20 is a diagrammatic elevational view similar to Fig. 18 except for the absence of the relay system and measures the wavefront error of transmissive filters over their bandpass; and

Fig. 21 is a diagrammatic elevational view of an alternative embodiment of the invention that uses an intervening telescope between the objective and CCD array to make full use of the available numerical aperture (NA) of the objective.

30

DETAILED DESCRIPTION OF THE INVENTION

The invention comprises a system and method for automatically performing dynamic screen testing on surfaces of optical components or systems or other surfaces that are at least partially specularly reflecting. The inventive system and method may be used for rapidly and accurately measuring optical parameters of a variety of optical elements and/or surfaces including, but not limited to, those of lenses and mold surfaces for forming them, flats, filters, and prisms. Lenses may be spherical, aspheric, or torics. The system is capable of measuring wavefronts, surface topography, radii of curvature, thickness, power and focal length, wavefront error in bandpass filters, and can exist in more or less complex forms depending on a selection of available features and desired range of operation, but in all of its forms, its principle of operation is the same.

Within less than a minute, for example, a measurement of radius of curvature can be made to an accuracy of less than 2.0 micrometer error, and other parametric measurements can be carried out with similar speeds. One form of the inventive system with the versatility of automatically measuring concave and convex elements over a wide parametric range and along different azimuths of rotation is shown in Figs. 1 where it is designated at 10. As can be seen in Fig. 1, along with Figs. 2-4, automatic measuring system 10 comprises a vertically oriented optical head 12, a Pentium based computer 14, a monitor 16, preferably color, and a keyboard 18 that is preferably an enhanced type. Optical head 12 is electrically connected to computer 14 via an interface board (not shown) located in one of computer 14's expansion slots. The interface board is configured in a well-known manner as an I/O board to: provide an electronic link between computer 14 and optical head 12 for the transmission of electrical and logic signals between them; provide drive signals to stepper motors located in optical head 12; and perform certain signal processing operations on raw signals generated by a video camera in optical head 12. Miscellaneous housekeeping chores may also be implemented via the arrangement. A separate framegrabber board may also be resident in one of the expansion slots of computer 14. Suitable cables (not shown) provide electrical links.

Keyboard 18 operates in the usual way to provide the operator with a means for communicating commands to computer 14, and monitor 16 displays a variety of system responses to the operator including measurement data, system status, and menu options to be selected for system control and direction. This is preferably done via a graphical user interface (GUI) in conjunction with a mouse 20 or other suitable device.

In addition, data and computer instructions in the form of programs may be transferred between operator and computer via one or more disk drives such as those shown typically at 34 in Fig. 1. The inventive system may also be networked in well-known manners.

On top of optical head 12 there is preferably provided a rotary stage 38 for receiving and supporting test optical elements in a reference plane so that they may be measured.

A fixed reference plane RP, as best seen in Fig. 5, is defined by three nylon balls 40 (only two of which are shown) that are precisely located in a V-groove formed in a nest ring 42 which also has a tapered conical tunnel that extends through to the interior of optical head 12 and is centered about its optical axis, OA, although not shown. In this connection, it is to be noted that the three nylon balls 40 also force the center of curvature of spherical surfaces to lie along the optical axis, OA, of the instrument. This is so because the various optical components comprising the optical head 12 are precisely aligned with the optical axis which, in turn, is made parallel to the mechanical axis of the optical head 12, and the mechanical axis is preferably made precisely perpendicular to the plane defined by the balls 40. If only spherical surfaces are to be measured, it is also possible to use a donut instead of the three nylon balls 40.

As can be seen in Fig. 5, test elements, such as that shown as 26, advantageously are automatically located in the reference plane by this three-ball location arrangement, even if slightly tilted about their own axis. When viewed from above, a circle centered on optical axis, OA, and drawn through the centers of each of them defines the semidiameter of the reference plane.

Referring now to Figs. 2 - 4, which show the interior of optical head 12, it is seen to further comprise a scanning head 50, which can be vertically moved along

optical axis, OA, via a translation stage 56 that, in turn, is driven via a conventional lead screw (not shown). The precision lead screw is driven by a precision stepper motor 58 fixed to the rear wall of optical head 12 and under command of computer 14. Translation stage 56 moves parallel to optical axis, OA, on a complementary
5 configured precision slide arrangement not shown in detail, but generally designated at 62 in Fig. 4. The pitch of the lead screw and the rotational steps of motor 58 are preferably selected in a well-known manner so that each step of the stepper motor 58 controllably moves the scanning head 50 up or down by a small fraction of a millimeter. The accuracy of this stepping motion can be enhanced by the use of
10 encoders which directly measure translation of stage 56 at each step. In addition to improving accuracy, encoders can also be utilized in minimizing inaccuracies due to wear, especially in the precision lead screw assembly 62.

Computer 14 is programmed in a well-known manner to keep track of the position of scanning head 50. In addition, limit switches may be provided to prevent
15 scanning head 50 from mechanically interfering with any structure beneath rotary table 38 and also to provide a locating signal indicating that scanning head 50 has reached its uppermost position when closed. In this manner, means are provided for precisely moving scanning head 50 along optical axis, OA, while at the same time providing a signal by which its vertical position can be monitored and controlled via computer 14.

Scanning head 50 comprises a number of components all of which travel
20 together along optical axis, OA. As best seen in Fig. 5, with occasional reference back to Figs. 2 - 4, these comprise a microscope objective 70, an adjustable diaphragm 71, preferably a pin hole, a collimated source of illumination 74 preferably in the form of a light emitting diode (LED), provided with suitable collimating optics, and a pellicle
25 beamsplitter 80 located between objective 70, source 74, and a video camera 76 to provide a split optical path between the three. The objective for camera 76 is preferably a pair of crossed lenticular screens with index mismatching material 77 sandwiched between them as best seen in Fig. 9. The crossed lenticular screens operate to provide the system with an array that is equivalent to a 2D array of spherical
30 lenses each of substantially the same focal length. The presence of the index material

provides a mechanism by which the focal length of the individual equivalent spherical lenses of the screen may be varied by a factor of four or more depending on the availability of the index of the material in accordance with the following relationship:

5
$$f = \frac{R}{n' - n}$$

where n' is the index of refraction of the lenticular screen material and n is the index of refraction of the material 77 between the crossed lenticular screens. Here, common indices range from approximately from 1.40 to 1.59.

10 It will be recognized that the lenticular screen may be replaced by an array of spaced apart mechanical apertures or holes, but with an attendant reduction in the dynamic range of the apparatus. This is so because the spherical lenses make for more tightly focused spots thereby making the amount of change in the local slope greater before spots overlap compared with what would be the case with pure mechanical
15 apertures. Also, use may be made of commercially available microlens arrays in place of the crossed lenticular screen and intermediate mismatching material.

Filters may also be used as needed to control the spectral output of the LED. Light source 74 preferably comprises an LED although a laser, fiber optic source, incandescent lamp, or discharge lamp may be used. Considerations in the choice of the
20 type of source to use include efficiency, cost, lifetime, ease of adjustment of light levels, and compactness. The spectral output of the source 74 should be considered because objective lens 70, being a microscope objective, is in the best case corrected for visible wavelengths. So, the spectral content of source 74 needs to be considered in terms of its impact on signal level because of any longitudinal aberrations introduced
25 at wavelengths outside the visible region. In addition, it is important to note that the part being measured may introduce chromatic aberrations if measured with a broader bandwidth source, and this may influence measurements in an undesirable way. Consequently, an LED is quite acceptable because it is a narrow source with no speckle or laser coherence problems. In addition, it is fairly monochromatic and easy

to modulate. The bandwidth of a narrow LED source for this purpose is typically tens of nanometers wide, not hundreds, and such devices are readily commercially available at low cost. In addition, they require low power to operate and have low heat dissipation.

5 The magnification, aperture, and NA of objective 70 are selected in well-known manners to operate in conjunction with the other system components so that adequate signal level is available over the desired area of the surface to be measured.

10 Having described the major system components of optical head 12, its operation will now be taken up referring to Figs. 5 -7. Optical head 12, comprising source 74, beamsplitter 80, objective lens 70, and lens array 78 with CCD camera 76, is mounted on translation stage 56 and moves along the optical axis of the head relative to the part under test. The part under test is mounted on an appropriate support, such as a three-point support nest that automatically centers spherical parts on the optical axis of the system.

15 Light in the form of a collimated beam with a plane wavefront 75 is projected along the optical axis via beamsplitter 80 through microscope objective 70 or other appropriate lens to illuminate the part under test with a predetermined wavefront, preferably spherical. The spherical wavefront is preferred, although not strictly required, so that subsequent calculations to be described are made simpler if the
20 reflected light is re-collimated parallel to the optical axis of the system. Light reflected from the part under test passes back through microscope lens 70, after which it passes through pellicle beamsplitter 80 towards array 78 of CCD camera 76. Lenticular array 78 is placed in front of the CCD active area, one focal length away from it, so that a series of sharp images are formed on the CCD array. This image or series of images as
25 the case may be, is passed via framegrabber 77 to computer 14 for analysis.

 When the system measuring head is positioned so that the focal point of the objective is located near the surface of the part under test as shown in Fig. 6, or near the center of curvature of the part under test as shown in Fig. 5, then the incoming nearly parallel light produces a series of spots on the CCD active area , $\Delta x = 0$ and
30 $\Delta y = 0$, the x and y displacements measured as deviations of a spot's centroid (See Fig.

8 which shows the variation of spot locations with focus position). The shifts in the pattern of spots is used to determine the topography of the surface under test as described hereinafter.

As best seen in Fig. 7, when the origin of the spherical wavefront is at some point other than the surface or its center of curvature (assuming a spherical surface), the return wavefront is no longer a plane wavefront and $\Delta x \neq 0$ and $\Delta y \neq 0$. As will be seen, mathematical analysis of these deviations leads to a measurement of the surface topography which, in turn, provides information on the radius of curvature of the part (if spherical), the "Spherical" and "Cylindrical" radii of curvature of a toric part (along with the angle between the major axes and a given reference axis), and the "Shape Factor" of an aspheric part, as well as other parameters which may be readily derived. For ease of interpretation, the overall shape can be expressed in various ways, including Zernike polynomials. Software performs this analysis and facilitates providing the results in many useful forms as, for example, contour plots, wire-frame models of deviation, direct readout of coefficients, direct readout of RMS surface form, direct readout of peak-to-valley difference, etc. Display screens are customizable for the engineering specialist or on-the-floor auditing and measurement for production. Custom processing capabilities are available using Visual Basic and an Object Linking And Embedding (OLE) interface.

Having described the components of the optical head and how plane and distorted wavefronts are generated in it, the mathematical algorithms used to analyze the information so generated will now be taken up. It is assumed that the part to be measured can be described, at least approximately, as having a radius of curvature **r**. **Z-bar**, the surface shape is then the sum of two components, a z-component related to the radius of curvature **r** and the sag **h(x,y)**, which is the departure of the surface from the base radius, **r**. Thus the surface may be represented by a sum of coefficients and functions, preferably as algebraic polynomials. Further, the focal length of the objective (or other lens) used to focus the collimated beam is **f**. The focal length of the array of lenslets is **F**. The separation between the array and the back principal plane of the objective is **d**, and the separation between the array of lenslets and the CCD is

nominally \mathbf{F} , but it may be different, in which case the actual separation is to be used in calculations in place of \mathbf{F} . Moreover, if a known perfect spherical part is measured, the actual distance between the CCD and the array of lenslets may be deduced from the resultant data and thereafter used in subsequent measurements.

- 5 Whenever the position of the optical head 12 is located so that the focus of the objective is very close to the surface of the part under test or its center of curvature, the reflected light will be very nearly collimated, and the result will be a series of well-focused spots on the CCD, with very nearly equal spacing between adjacent spots (assuming the lenslets in the array are nearly equally spaced). There will, in general,
- 10 be a shift between the location of a given spot and the spot one obtains when truly collimated light is incident on the CCD camera with its lenslet array. So long as the light is nearly collimated, there is no great difficulty in associating any given deviated spot with the position of an undeviated spot. If necessary, one such spot can be decreased in intensity or otherwise identified by eccentricity in shape, intensity, or
- 15 location so as to provide a reference point to help identify spot correspondence. (The appearance of a series of undeviated spots can easily be generated by placing a plane first-surface mirror atop the lens nest, or use a reflection from the unused "arm" of light reflected from the beamsplitter). The size and direction of the deviation of this spot from the expected position provides information on the angular shift of the ray of
- 20 light at that point. This can be related to the difference in the part under test between the expected slope for a spherical surface and the actual slope. From this is derived the deviation in surface height between a spherical reference surface (whose radius is equal to the distance between the "Surface" location and the present position of the translation stage) and the true surface. Note that the actual surface \mathbf{Z} -bar will always
- 25 be substantially the same regardless of the location of the objective focus with respect to the surface provided sensible deviations are being measured.

The difference in height $h(\mathbf{x}_{pij}, \mathbf{y}_{pij})$ of the surface of the part under test is expressed as a polynomial in two variables, \mathbf{x}_{pij} and \mathbf{y}_{pij} :

$$h(\mathbf{x}_{pij}, \mathbf{y}_{pij}) = a_{10}\mathbf{x}_{pij} + a_{01}\mathbf{y}_{pij} + a_{11}\mathbf{x}_{pij}\mathbf{y}_{pij} + a_{20}\mathbf{x}_{pij}^2 + a_{02}\mathbf{y}_{pij}^2 + \dots$$

Here the subscript “p” denotes a coordinate on the surface of the part (without the “p” the coordinates **x** and **y** refer to coordinates in the CCD plane). The subscripts **i** and **j** refer to the numbering of the coordinates/spots. The angular deviation ϵ_{xij} at a spot (x_p, y_p) measured along the x-direction is given by:

$$\left. \frac{\partial h}{\partial x_p} \right|_{(x_{pj}, y_{pj})} = \epsilon_{xij}$$

Similarly, the angular deviation ϵ_{yij} along the y-direction is given by:

$$\left. \frac{\partial h}{\partial y_p} \right|_{(x_{pj}, y_{pj})} = \epsilon_{yij}$$

Straightforward calculation (using, as an example, polynomials only to second order) then gives:

$$\epsilon_{xij} = a_{10} + 2a_{20}x_{pij} + a_{11}y_{pij}$$

$$\epsilon_{yij} = a_{01} + a_{11}x_{pij} + 2a_{02}y_{pij}$$

The relationship between these slopes and the observed shifts of the spots seen by the CCD can be related by the following expressions, obtained from geometrical optics. The value of the radius of curvature, **r**, should be set equal to the separation between the positions of the translation stage at which the spot shifts are minimized :

$$\varepsilon_{xij} = \Delta x_{ij} \frac{f}{2Fr} = a_{10} + 2a_{20}x_{pij} + a_{11}y_{pij}$$

$$\varepsilon_{yij} = \Delta y_{ij} \frac{f}{2Fr} = a_{01} + a_{11}x_{pij} + 2a_{02}y_{pij}$$

Finally, the coordinates on the surface of the (concave) part are related to those in the plane of the CCD by the expressions:

$$x_{pij} = -\left(\frac{r}{f}\right)x_{ij} + \Delta x_{ij} \left\{ \left(\frac{1}{F}\right) \left[\frac{dr}{f} - (r+f) \right] \right\}$$

$$y_{pij} = -\left(\frac{r}{f}\right)y_{ij} + \Delta y_{ij} \left\{ \left(\frac{1}{F}\right) \left[\frac{dr}{f} - (r+f) \right] \right\}$$

Here Δx_{ij} and Δy_{ij} are the shifts in the **x**- and **y**- directions of the **i,j**th spot. (For convex parts we replace **r** by $-r$). The index **i** runs from **0** to **N**, while the index **j** runs from **0** to **M**.

Next, the values of the coefficients of the polynomials are calculated by performing a least-square fit of the observed shifts of the spots to the shape of the surface, using the above relations. If $\varepsilon_{xij} \equiv \xi_{ij}$ and $\varepsilon_{yij} \equiv \eta_{ij}$, then this least-square fit can be accomplished by solving the matrix equation:

$$\begin{bmatrix} NM & 0 & \sum y_{pij} & 2\sum x_{pij} & 0 \\ 0 & NM & \sum x_{pij} & 0 & 2\sum y_{pij} \\ \sum y_{pij} & \sum x_{pij} & \sum (y_{pij}^2 + x_{pij}^2) & 2\sum x_{pij}y_{pij} & 2\sum x_{pij}y_{pij} \\ 2\sum x_{pij} & 0 & 2\sum x_{pij}y_{pij} & 4\sum x_{pij}^2 & 0 \\ 0 & 2\sum y_{pij} & 2\sum x_{pij}y_{pij} & 0 & 4\sum y_{pij}^2 \end{bmatrix} \begin{bmatrix} a_{10} \\ a_{01} \\ a_{11} \\ a_{20} \\ a_{02} \end{bmatrix} = \begin{bmatrix} \sum \xi_{ij} \\ \sum \eta_{ij} \\ \sum (y_{pij}\xi_{ij} + x_{pij}\eta_{ij}) \\ 2\sum x_{pij}\xi_{ij} \\ 2\sum y_{pij}\eta_{ij} \end{bmatrix}$$

The relevant expressions for carrying the surface profile out to fourth order are longer and more daunting. The slope equations become:

$$\xi_{ij} = a_{10} + 2a_{20}x + a_{11}y + 3a_{30}x^2 + 2a_{21}xy + a_{12}y^2 + 4a_{40}x^3 + 3a_{31}x^2y + 2a_{22}xy^2 + a_{13}y^3$$

$$\eta_{ij} = a_{01} + a_{11}x + 2a_{02}y + a_{21}x^2 + 2a_{12}xy + 3a_{03}y^2 + a_{31}x^3 + 2a_{22}x^2y + 3a_{13}xy^2 + 4a_{04}y^3$$

5

(To save space, the subscripts on the variables have been suppressed. All x 's are x_{pij} and all y 's are y_{pij} , all variables on the surface of the part.). The matrix corresponding to the second-order matrix above is a 14 X 14 matrix. It will not fit on this page legibly, so it is broken down by a vertical fissure into two halves, which are reproduced below, the left side first (Note that the matrix is symmetrical about the diagonal.

10

Again, the subscripts have been suppressed for the purposes of clarity.):

$$\begin{bmatrix} NM & 0 & 2\sum x & \sum y & 0 & 3\sum x^2 & 2\sum xy \\ 0 & NM & 0 & \sum x & 2\sum y & 0 & \sum x^2 \\ 2\sum x & 0 & 4\sum x^2 & 2\sum xy & 0 & 6\sum x^3 & 4\sum x^2y \\ \sum y & \sum x & 2\sum xy & \sum (x^2 + y^2) & 2\sum xy & 3\sum x^2y & \sum (2xy^2 + x^3) \\ 0 & 2\sum y & 0 & 2\sum xy & 4\sum y^2 & 0 & 2\sum x^2y \\ 3\sum x^2 & 0 & 6\sum x^3 & 3\sum x^2y & 0 & 9\sum x^4 & 6\sum x^3y \\ 2\sum xy & \sum x^2 & 4\sum x^2y & \sum (2xy^2 + x^3) & 2\sum x^2y & 6\sum x^3y & \sum (4x^2y^2 + x^4) \\ \sum y^2 & 2\sum xy & 2\sum xy^2 & \sum (2x^2y + y^3) & 4\sum xy^2 & 3\sum x^2y^2 & 2\sum (xy^3 + x^3y) \\ 0 & 3\sum y^2 & 0 & 3\sum xy^2 & 6\sum y^3 & 0 & 3\sum x^2y^2 \\ 4\sum x^3 & 0 & 8\sum x^4 & 4\sum x^3y & 0 & 12\sum x^5 & 8\sum x^4y \\ 3\sum x^2y & \sum x^3 & 6\sum x^3y & \sum (3x^2y^2 + x^4) & 2\sum x^3y & 9\sum x^4y & \sum (6x^3y^2 + x^5) \\ 2\sum xy^2 & 2\sum x^2y & 4\sum x^2y^2 & 2\sum (xy^3 + x^3y) & 4\sum x^2y^2 & 6\sum x^3y^2 & \sum (4x^2y^3 + 2x^4y) \\ \sum y^3 & 3\sum xy^2 & 2\sum xy^3 & \sum (3x^2y^2 + y^4) & 6\sum xy^3 & 3\sum x^2y^3 & \sum (2xy^4 + 3x^3y^2) \\ 0 & 4\sum y^3 & 0 & 4\sum xy^3 & 8\sum y^4 & 0 & 4\sum x^2y^3 \end{bmatrix}$$

The right half of the matrix is:

$$\begin{bmatrix} \sum y^2 & 0 & 4\sum x^3 & 3\sum x^2y & 2\sum xy^2 & \sum y^3 & 0 \\ 2\sum xy & 3\sum y^2 & \sum x^3 & \sum x^2y & 2\sum xy^2 & 3\sum y^3 & 4\sum y^4 \\ 2\sum xy^2 & 0 & 8\sum x^4 & 6\sum x^3y & 4\sum x^2y^2 & 2\sum xy^3 & 0 \\ \sum (2x^2y+y^3) & 3\sum xy^2 & 4\sum x^3y & \sum (3x^2y^2+x^4) & 2\sum (xy^2+x^3y) & \sum (y^2+3x^2y^2) & 4\sum xy^3 \\ 4\sum xy^2 & 6\sum y^3 & 0 & 2\sum x^3y & 4\sum x^2y^2 & 6\sum xy^3 & 8\sum y^4 \\ 3\sum x^2y^2 & 0 & 12\sum x^5 & 9\sum x^4y & 6\sum x^3y^2 & 3\sum x^2y^3 & 0 \\ 2\sum (xy^2+x^2y) & 3\sum x^2y^2 & 8\sum x^4y & \sum (6x^3y^2+x^5) & \sum (4x^2y^2+2x^4y) & \sum (2xy^2+3x^2y^2) & 4\sum x^2y^3 \\ \sum (4x^2y^2+y^4) & 6\sum xy^3 & 4\sum x^3y^2 & \sum (3x^2y^2+2x^4y) & \sum (2xy^2+4x^3y^2) & \sum (y^2+6x^2y^2) & 8\sum xy^4 \\ 6\sum xy^3 & 9\sum y^4 & 0 & 3\sum x^3y^2 & 6\sum x^2y^3 & 9\sum xy^4 & 12\sum y^5 \\ 4\sum x^3y^2 & 0 & 16\sum x^6 & 12\sum x^5y & 8\sum x^4y^2 & 4\sum x^3y^3 & 0 \\ \sum (3x^2y^2+2x^4y) & 3\sum x^2y^2 & 12\sum x^5y & \sum (9x^4y^2+x^6) & \sum (6x^3y^2+2x^5y) & 3\sum (x^2y^2+x^4y^2) & 4\sum x^2y^3 \\ \sum (2xy^2+4x^3y^2) & 6\sum xy^3 & 8\sum x^4y^2 & \sum (6x^3y^2+2x^5y) & 4\sum (x^2y^2+x^4y^2) & \sum (2xy^2+6x^2y^2) & 8\sum x^2y^4 \\ \sum (y^2+6x^2y^2) & 9\sum xy^4 & 4\sum x^3y^3 & 3\sum (x^2y^2+x^4y^2) & \sum (2xy^2+6x^3y^2) & \sum (y^2+9x^2y^2) & 12\sum xy^5 \\ 8\sum xy^4 & 12\sum y^5 & 0 & 4\sum x^3y^3 & 8\sum x^2y^4 & 12\sum xy^5 & 16\sum y^6 \end{bmatrix}$$

- 5 The accompanying “Results” column vector is a 14 X 1 expression:

$$\begin{bmatrix} \sum \xi_{ij} \\ \sum \eta_{ij} \\ 2\sum x_{pij}\xi_{ij} \\ \sum (y_{pij}\xi_{ij} + x_{pij}\eta_{ij}) \\ 2\sum y_{pij}\eta_{ij} \\ 3\sum x_{pij}\xi_{ij} \\ \sum (2x_{pij}y_{pij}\xi_{ij} + x_{pij}^2\eta_{ij}) \\ \sum (y_{pij}^2\xi_{ij} + 2x_{pij}y_{pij}\eta_{ij}) \\ 3\sum x_{pij}^2\eta_{ij} \\ 4\sum x_{pij}^3\xi_{ij} \\ \sum (3x_{pij}^2y_{pij}\xi_{ij} + x_{pij}^3\eta_{ij}) \\ 2\sum (x_{pij}y_{pij}^2\xi_{ij} + x_{pij}^2y_{pij}\eta_{ij}) \\ \sum (y_{pij}^3\xi_{ij} + 3x_{pij}y_{pij}^2\eta_{ij}) \\ 4\sum y_{pij}^3\eta_{ij} \end{bmatrix}$$

As will be discussed in more detail hereinafter, the calculations can be extended for surfaces of any power, but it should be noted that the number of terms grows very rapidly. For a surface expressed in powers up to the n th order there will be

5 $(n + 1)(n + 2)/2$ terms, and the required matrix expression will be $Q \times Q$, where

$$Q = \{(n + 1)(n + 2)/2\} - 1.$$

Once the coefficients have been derived, it is a simple matter to calculate the surface departure from a sphere, and to calculate the rms surface departure, the peak-to-valley difference, and any other measure desired. The size of the reference sphere
10 against which the surface is compared, it should be noted, has a radius equal to the distance between the "Surface" location (position at which the focus of the Objective lens coincides with the surface of the Part Under Test) and the present location of the focus of the objective (in general, there will be no result unless this location is either near the "Surface" location itself, or is near the Center of Curvature of the part).

15 The departure from sphericity of the surface can be expressed in the form of Zernike polynomials (which are simply appropriately weighted combinations of surface polynomials), which are commonly used descriptors of optical elements, useful in the study of aberrations.

The radius of curvature of a spherical surface can be measured in several ways.
20 The simplest and most direct is to measure the distance between the two "crossing points" of the second order coefficients. This distance is equal to the radius of curvature of the spherical surface. Provided the part is aligned so that the optical axis runs through the center of the spherical surface, the plots of a_{02} and a_{20} as a function of position z will be identical, falling to zero at the same positions near the "Surface" and
25 the "Center of Curvature" (CoC) locations. This is a very direct and robust measurement, since it will yield the radius of curvature even if the instrument is not properly calibrated. That is, the relationship between the spot shifts Δx_{ij} and Δy_{ij} and the deviation of the surface from a true sphere might not be correctly calculated because the distances or focal lengths might not be properly entered, but (as long as the
30 focus scale of z measurement is properly calibrated) the separation between the

crossing points will give the radius of curvature in all cases. In fact, this method can be used to check the calibration of the translation stage.

The radius can also be obtained from the variation of the coefficients a_{20} and a_{02} with position, z . Again, assuming that both curves coincide (so that we may speak of them as the single function, $a_2(z)$), and assuming z is measured from the Surface position, the relationship between $a_2(z)$ and z will be given by:

$$\frac{1}{r} = \frac{1}{z} + (a_{20} + a_{02}) = \frac{1}{z} + 2a_2$$

Which can be re-arranged to give

$$a_2 = \frac{1}{2r} - \frac{1}{2z}$$

A plot of a_2 versus position can yield the radius in one of two ways. If a_2 is plotted against z , then one can derive the radius from the slope:

$$r = \frac{1}{2 \left[\frac{\partial a_2}{\partial z} \right]_{z=r}}$$

A plot of a_2 vs. $1/z$ gives the result more directly, since the intercept, by the above equation, is $1/2r$. Both of these methods can be used to calibrate the instrument, if the measurement is performed with a known spherical standard. (The radius of the part need not even be known, since the coefficient of $1/z$ must be $-1/2$. All one needs to know is that the part is spherical.)

Finally, if the part is known to be spherical, but the plots of a_{20} and a_{02} do not overlap, then this separation can be used to calculate the decentering of the part (i.e. – the separation between the center as defined by the fixture for the part and the optical

axis of the measuring head). One can express the coefficients a_{20} , a_{02} , and a_{11} as a function of the center location (x_0, y_0) , or vice-versa:

$$a_{20} = \frac{1}{2} \left[\frac{1}{r_1} - \frac{1}{r_0} + \frac{3}{2} \frac{x_0^2 + y_0^2}{r_1^3} \right]$$

$$a_{02} = \frac{1}{2} \left[\frac{1}{r_1} - \frac{1}{r_0} + \frac{1}{2} \frac{x_0^2 + y_0^2}{r_1^3} \right]$$

5

$$a_{11} = \frac{x_0 y_0}{r_1^3}$$

$$x_0 = r_1^{3/2} \sqrt{\sqrt{(a_{20} - a_{02})^2 - a_{11}^2} + (a_{20} - a_{02})}$$

$$y_0 = \frac{a_{11} r_1^{3/2}}{\sqrt{\sqrt{(a_{20} - a_{02})^2 - a_{11}^2} + (a_{20} - a_{02})}}$$

- 10 When the surface has a well-defined geometrical form which is nearly spherical, the coefficients can be analyzed to yield information about that shape. A good example is a toric surface, in which the surface resembles a slice from the outer edge of a torus. Such a surface has one radius of curvature along one axis and a different radius of curvature along the axis perpendicular to the first. A toric shape is
- 15 commonly used in contact lenses to correct for astigmatism. A sphere is a special case of a toric in which the two radii of curvature are equal.

The general equation for a toric can be given in the form:

$$x^2 + y^2 + z^2 + R^2 - r^2 - 2R\sqrt{x^2 + y^2} = 0$$

These variables **x**, **y**, and **z** are different from those used in the rest of this paper, and should not be confused with them. This equation describes a circle of radius **r** which is rotated about an axis in the plane of the circle, lying a distance **R** from the center of the circle. The familiar “doughnut” shape is generated when **R** > **r**. In this case the large circle of radius **R** lies in the **xy** plane, and the axis **z** runs through the center of the doughnut “hole”. The toric surface used in lenses lies near the outer extremity of such a doughnut shape, near the point a distance **R** + **r** from the center along the **x** or **y** axis. A segment near this point lying in the **xy** plane will have a radius of curvature of **r** + **R**. A segment lying perpendicular to this plane, in the **xz** plane, for instance, will have radius of curvature **r**. In practice, **R** is usually significantly smaller than **r**, so the “doughnut” is re-entrant, and very nearly resembles a sphere. The axis along which the radius is equal to **R** + **r**, called the Cylindrical axis (as **R** + **r** is called the Cylindrical Radius of Curvature) may lie rotated by some angle ϕ from the Zero axis of reference of the SMI. The axis along which the radius measures **r** (the Spherical Radius of Curvature, measured along the Spherical axis) is always perpendicular to the Cylindrical axis.

For such a part plots of the coefficients **a₀₂**, **a₂₀**, and **a₁₁** as a function of position **z** look somewhat different than in the spherical case. **a₁₁** is still constant, but is not equal to zero. The coefficients **a₀₂** and **a₂₀** will look similar to each other, maintaining a fixed separation, but will not, in general, coincide. The two plots will, in fact, coincide if ϕ equals 45°. The values of these three coefficients, along with a knowledge of the distance from the Surface location at which the coefficients are determined, will give the values of **r**, **R**, and ϕ . (The plots of **a₀₂** and **a₂₀** will still

coincide at the Surface location, so there is no ambiguity). The relevant equations are:

$$r = \left[\frac{1}{z} + (a_{20} + a_{02}) + \sqrt{(a_{20} - a_{02})^2 + (a_{11})^2} \right]^{-1}$$

$$R = \frac{2r^2 \sqrt{(a_{20} - a_{02})^2 + (a_{11})^2}}{1 - 2r \sqrt{(a_{20} - a_{02})^2 + (a_{11})^2}}$$

$$\phi = \frac{1}{2} \tan^{-1} \left(\frac{a_{11}}{a_{20} - a_{02}} \right)$$

5

In order to use these equations one need only know the values of the coefficients at a single location (whose position relative to the Surface must also be known). It is useful to obtain measurements at several positions, however, since then one can calculate the functional form via a least-square method and thus compensate for random errors in measurement. We find by experience that such random errors can be significant, so looking at the trend allows us to obtain a more accurate result than we can through measurement at any one position. This is also an advantage of this method of performing Shack-Hartmann tests over static methods. This same method can be used for the accurate determination of all coefficients up to the order used for the fitting of the shift data. Coefficients \mathbf{a}_{nm} in which either \mathbf{n} or \mathbf{m} is odd will be constant with position \mathbf{z} , while those for which both \mathbf{n} and \mathbf{m} are even can be expressed in the form $(\text{constant}) - (\text{constant}')/z^{(n+m-1)}$. A least square fit to a series of measurements of $\mathbf{a}_{nm}(\mathbf{z})$ can easily be performed using matrix methods, yielding a robust result that is insensitive to noise.

20

As another example, the value of the Shape Factor of an aspheric part can be obtained by using the values of the fourth order coefficients. The Shape Factor is given by $\kappa + 1$, where κ is the "Conic Constant". The value of $\kappa + 1$ equals 1 for a

sphere. If the value is greater than 1 or between 1 and 0 the result is an ellipse. A value of $\kappa + 1 = 0$ gives a parabola, while a value less than zero yields a hyperbola.

Provided the axis of the part is aligned with the axis of the optical system and centered, the Shape Factor $\kappa + 1$ is given by the fourth order coefficients $a_{40} = a_{04} =$

5 $a_{22}/2 = a_4$ by the expression:

$$\kappa + 1 = 8r^3 a_4 + 1$$

Here r is, of course, the value of the radius of curvature obtained from crossing-point data, or one of the other methods noted above.

For practical measurements, it may sometimes be necessary to make small
10 corrections to these mathematically derived formulas.

Beyond spheres and torics, shapes of increasing complexity can be studied by extending the methodology of the invention. By doing this, "atoric" shapes (shapes that are toric when observed near the optical axis, but which depart from that shape as you get farther from the axis) can be examined as well as more general shapes. There
15 is a straightforward method for determining the shapes of parts along an arbitrarily chosen azimuth, and it is the method used in plotting the radius of curvature maps. From a position z along the direction of travel, and the surface parameters a_{nm} can be measured. Then the surface can be *constructed* by adding the sag of a spherical surface of radius z (the reference sphere) to the sag determined by these parameters. From this
20 the radius of curvature can be calculated if desired.

Thus, the method for measuring spherical parts, and in determining the coefficients of toric parts can be extended to more complex parts, measured to higher orders. The difference lies in the way the measurements are made. The great strength of the invention is the use made of not only the shifts characteristic of the surface
25 shape at *one* reference position, but at a series of them. What has been plotted has been the values of the second order coefficients a_{20} , a_{11} , and a_{02} as a function of z . A least-square fit of this data to the theoretical functional form was then performed, and results were obtained for the toric parameters that are unusually reproducible. This

was possible by using least-square fitting, which allows for a sort of averaging over positions, "averaging out" the statistical errors at each individual position and obtaining a much more stable result. The plots of $\mathbf{a}_{20}(\mathbf{z})$, $\mathbf{a}_{11}(\mathbf{z})$, and $\mathbf{a}_{02}(\mathbf{z})$ might not describe precisely defined curves, but the first and last of these can be fit to the

- 5 functional form **constant** + $1/2z$ (with a different constant in each case) and the middle one to **constant'** and very good fits and results can be obtained. Even use of the knowledge that the slopes vs. $1/z$ must be $1/2$ to perform fine-tuning on the magnification of the invention has been used. It is this combination of knowledge of the functional form of $\mathbf{a}_{nm}(\mathbf{z})$ with least-square fitting that gives us such reliable and
- 10 stable results.

- This procedure can be carried through to surface plotting, radius-mapping, and aspheric (and atoric) calculations since there is more information present than use is made of in just spherical and toric measurements, and this information resides in higher-order terms. By fitting them, via least-square formulations, to their expected
- 15 functional forms, instead of to the variations otherwise seen at a single point, advantage of multiple measurements to average out the error can be made. Instead of plotting different surface shapes for the results at each position \mathbf{z} , a single set of parameters is determined which is used to plot surface variation, radius map, etc. for *all* positions \mathbf{z} . One practical result is that the maps and results do not change as
- 20 when moving through \mathbf{z} – there is a single, well-defined shape and set of maps. These results are much more reproducible and stable.

To accomplish this, the functional forms that are to be expected need to be known or estimated in a rational way. On the surface, this seems difficult. Surely, it is different for a spherical part than for an aspheric part than for a toric, or an atoric part.

- 25 However, the answer is surprisingly simple. The expected forms for *all* the higher order terms are extremely simple, and can be written down without *any* special knowledge of the expected shape of the part. Using the expected forms written below, it is a simple matter to perform least-square fitting over a range of \mathbf{z} values and obtain averaged results for further calculation.

The key to this lies in realizing that the shape the surface actually has is a constant thing. It is entirely independent of the position \mathbf{z} at which the measurement takes place. This is true if the surface is spherical, aspheric, toric, or anything else. The coefficients \mathbf{a}_{nm} will be functions of \mathbf{z} , but when you calculate the sag of the surface (by adding the sag of the reference sphere of radius \mathbf{z} to the sum of $\mathbf{a}_{nm}\mathbf{x}^n\mathbf{y}^m$), you should end up with the same shape, since the surface always has the same shape, regardless of where you are standing when you measure it.

The sag of the reference surface measured at a position \mathbf{z} (and presumed to be equal to zero at the origin, $\mathbf{x} = 0, \mathbf{y} = 0$) can be written in the following way (as we have shown often enough):

$$Sag(z) = z - \sqrt{z^2 - (x^2 + y^2)}$$

$$Sag(z) = z \left[1 - \sqrt{1 - \frac{(x^2 + y^2)}{z^2}} \right]$$

$$Sag(z) = \frac{x^2 + y^2}{2z} + \frac{(x^2 + y^2)^2}{8z^3} + \frac{(x^2 + y^2)^3}{16z^5} + \dots$$

$$Sag(z) = \frac{x^2}{2z} + \frac{y^2}{2z} + \frac{x^4}{8z^3} + \frac{x^2y^2}{4z^3} + \frac{y^4}{8z^3} + \frac{x^6}{16z^5} + \frac{3x^4y^2}{16z^5} + \frac{3x^2y^4}{16z^5} + \frac{y^6}{16z^5} + \dots$$

It will be obvious that the only way that the surface shape obtained by adding this sag to the sag made up of the terms $\mathbf{a}_{nm}\mathbf{x}^n\mathbf{y}^m$ can be independent of \mathbf{z} , regardless of the shape of the surface, is if the terms \mathbf{a}_{nm} can be written in the following forms:

$$a_{00}(z) = \text{const}$$

$$a_{10}(z) = \text{const}$$

$$a_{01}(z) = \text{const}$$

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$$a_{20}(z) = \text{const} - \frac{1}{2z}$$

$$a_{11}(x) = \text{const}$$

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$$a_{02}(z) = \text{const} - \frac{1}{2z}$$

$$a_{30}(z) = \text{const}$$

$$a_{21}(z) = \text{const}$$

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$$a_{12}(z) = \text{const}$$

$$a_{03}(z) = \text{const}$$

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$$a_{40}(z) = \text{const} - \frac{1}{8z^3}$$

$$a_{31}(z) = \text{const}$$

$$a_{22}(z) = \text{const} - \frac{1}{4z^3}$$

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$$a_{13}(z) = \text{const}$$

$$a_{04}(z) = \text{const} - \frac{1}{8z^3}$$

In the above it should be evident that the constants are generally different. Frequently most of them are equal to zero. The fact that the coefficients should have the above forms receives some verification from the theoretical forms for the coefficients of a toric part as given.

$$a_{20} = \frac{1}{2} \left\{ \frac{1}{r} - \frac{1}{z} - A [\sin \phi]^2 \right\}$$

$$a_{02} = \frac{1}{2} \left\{ \frac{1}{r} - \frac{1}{z} - A [\cos \phi]^2 \right\}$$

$$a_{11} = A \sin \phi \cos \phi$$

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$$A \equiv \frac{R}{r(r+R)}$$

$$a_{40} = \frac{1}{8} \left\{ \frac{1}{(r+R)^3} - \frac{1}{z^3} + \frac{2R}{r(r+R)^3} \cos^2 \phi + \left[\frac{R^2}{r^2(r+R)^3} + \frac{R}{r^3(r+R)} \right] \cos^4 \phi \right\}$$

$$a_{04} = \frac{1}{8} \left\{ \frac{1}{(r+R)^3} - \frac{1}{z^3} + \frac{2R}{r(r+R)^3} \sin^2 \phi + \left[\frac{R^2}{r^2(r+R)^3} + \frac{R}{r^3(r+R)} \right] \sin^4 \phi \right\}$$

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$$a_{31} = \frac{R \cos \phi \sin \phi}{2r(r+R)} \left\{ \frac{1}{(r+R)^2} + \left[\frac{R}{r(r+R)^2} + \frac{1}{r^2} \right] \cos^2 \phi \right\}$$

$$a_{13} = \frac{R \cos \phi \sin \phi}{2r(r+R)} \left\{ \frac{1}{(r+R)^2} + \left[\frac{R}{r(r+R)^2} + \frac{1}{r^2} \right] \sin^2 \phi \right\}$$

$$a_{22} = \frac{1}{4(r+R)} \left\{ \frac{1}{(r+R)^2} + \frac{R}{r(r+R)^2} + \cos^2 \phi \sin^2 \phi \frac{3R}{2r^2} \left[\frac{R}{(r+R)^2} + \frac{1}{r} \right] \right\} - \frac{1}{4z^3}$$

These coefficients are all of the form listed above. (The third order coefficients \mathbf{a}_{30} , \mathbf{a}_{21} , \mathbf{a}_{12} , and \mathbf{a}_{03} are all equal to zero, which is a constant). It is important to realize that *atoric* parts are also of this form. One can convince oneself that spherical parts are, as well, and even perfectly flat parts.

This brings up the question of how to determine the coefficients. This should be done in a manner similar to the second-order coefficients we determine for toric measurements. We perform a least-square fit in which we force the slopes of the relevant parameters to be the theoretically fixed values. Most of the coefficients can be calculated by simply taking the average over the values obtained at each position \mathbf{z} . This will be true for all terms that do not show up in the expansion of the reference sphere sag. In other words:

$$\langle a_{nm} \rangle_{average} \equiv \frac{1}{N} \sum_{n=1}^N a_{nm}(z_n)$$

- 15 This will hold true for \mathbf{a}_{00} , \mathbf{a}_{10} , \mathbf{a}_{11} , \mathbf{a}_{30} , \mathbf{a}_{21} , \mathbf{a}_{12} , \mathbf{a}_{03} , \mathbf{a}_{31} , \mathbf{a}_{13} , etc.

Now, you can determine the second order coefficients from:

$$\begin{bmatrix} K & \sum_k \frac{1}{z_k} & 0 \\ \sum_k \frac{1}{z_k} & 2 \sum_k \left(\frac{1}{z_k} \right)^2 & \sum_k \frac{1}{z_k} \\ 0 & \sum_k \frac{1}{z_k} & K \end{bmatrix} \begin{bmatrix} offset_{20} \\ slope \\ offset_{02} \end{bmatrix} = \begin{bmatrix} \sum_k a_{20}(z_k) \\ \sum_k \frac{a_{20}(z_k) + a_{02}(z_k)}{z_k} \\ \sum_k a_{02}(z_k) \end{bmatrix}$$

We then get $\mathbf{a}_{20}(\mathbf{z}) = \text{offset}_{20} + \text{slope}/z$ and $\mathbf{a}_{02}(\mathbf{z}) = \text{offset}_{02} + \text{slope}/z$. But if we are confident of our alignment and magnification factors, then the slope is *known* to be $-1/2$, and we can determine the offsets from the much simpler formula:

$$\langle \text{offset}_{20} \rangle_{\text{average}} = \frac{1}{N} \sum_{n=1}^N \left[a_{20}(z_n) + \frac{1}{2z_n} \right]$$

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$$\langle \text{offset}_{02} \rangle_{\text{average}} = \frac{1}{N} \sum_{n=1}^N \left[a_{02}(z_n) + \frac{1}{2z_n} \right]$$

In fact, we can say that if we know that the slope of a term should be $-1/bz^c$, then we can write the expression for the average value of the offset as:

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$$\langle \text{offset}_{nm} \rangle_{\text{average}} = \frac{1}{N} \sum_{k=1}^N \left[a_{nm}(z_k) + \frac{1}{bz_k^c} \right]$$

Once these coefficients have all been determined, all that must be done to calculate the shape of the surface is to choose a point \mathbf{z} and add the sag of the reference surface at a point \mathbf{z} to the sum of the terms $\mathbf{a}_{nm}(\mathbf{z})\mathbf{x}^n\mathbf{y}^m$. Because of the restrictions we have placed on these terms, you are guaranteed that the surface thus generated will be independent of \mathbf{z} , at least to the highest order for which you have generated terms. In fact, an alternative way to calculate the surface profile is simply to add up the sum of $\mathbf{a}_{nm}\mathbf{x}^n\mathbf{y}^m$ for the *constant* terms (\mathbf{a}_{00} , \mathbf{a}_{10} , \mathbf{a}_{01} , \mathbf{a}_{11} etc.) and the sums of the “offset” parts of the *varying* terms -- i.e. $\text{offset}_{20}\mathbf{x}^2 + \text{offset}_{02}\mathbf{y}^2 + \text{offset}_{40}\mathbf{x}^4 + \dots$. This procedure can also be used in calculating derived quantities, as well. Calculation of aspheric coefficients and shape factors can still be carried out as before, but we now use these

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“scan-averaged” values, rather than values obtained only at one position \mathbf{z} . The result should be stabler, more accurate values at all locations.

The invention can also be used to determine the amount of offset in lathe-turned spherical parts. Manufacturers are using lathes to turn spherical parts, but if the center of the sphere which the computerized lathe tool is moving along does not coincide with the axis of the lathe, then there will be a problem. Instead of generating a sphere the surface will be something else (a variety of torus, but still very different from the shape usually called by that name). An axial slice through such a part will either resemble a gothic arch or will have a “cusp” in the center, depending upon whether the offset is positive or negative.

Such an offset can be determined from the following analysis. If we take \mathbf{z} as the coordinate along the part (and lathe) axis, and $\mathbf{r} = (\mathbf{x}^2 + \mathbf{y}^2)^{1/2}$ as the radial dimension, then the “Sag” \mathbf{z} of a spherical surface of radius \mathbf{R} is given by:

$$z = R - \sqrt{R^2 - r^2} = R \left\{ 1 - \sqrt{1 - \left(\frac{x}{R}\right)^2 - \left(\frac{y}{R}\right)^2} \right\}$$

If the axis is offset by a distance \mathbf{g} , then the sag becomes:

$$z = R \left\{ 1 - \sqrt{1 - \left(\frac{r-g}{R}\right)^2} \right\}$$

The difference in sag between the surface of such a decentered part and a perfectly centered Reference Sphere of radius \mathbf{R}_0 is given by $\Delta\mathbf{z}$:

$$\Delta z = R_0 \left\{ 1 - \sqrt{1 - \left(\frac{r}{R_0}\right)^2} \right\} - R \left\{ 1 - \sqrt{1 - \left(\frac{r-g}{R}\right)^2} \right\}$$

If we expand the terms containing the square roots we obtain:

$$\Delta z = (R_0 - R) - R_0 \left\{ 1 - \frac{1}{2} \left(\frac{r}{R_0} \right)^2 - \frac{1}{8} \left(\frac{r}{R_0} \right)^4 - \frac{1}{16} \left(\frac{r}{R_0} \right)^6 + \dots \right\} + R \left\{ 1 - \frac{1}{2} \left(\frac{r-g}{R} \right)^2 - \frac{1}{8} \left(\frac{r-g}{R} \right)^4 - \frac{1}{16} \left(\frac{r-g}{R} \right)^6 + \dots \right\}$$

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$$\Delta z = \frac{1}{2} \left[\frac{r^2}{R_0} - \frac{(r-g)^2}{R} \right] + \frac{1}{8} \left[\frac{r^4}{R_0^3} - \frac{(r-g)^4}{R^3} \right] + \frac{1}{16} \left[\frac{r^6}{R_0^5} - \frac{(r-g)^6}{R^5} \right] + \dots$$

If we further assume that $g \ll r$ (as we expect), then we can further simplify this to:

$$\Delta z \cong \frac{r^2(R - R_0) + 2grR_0}{2RR_0} + \frac{r^4(R^3 - R_0^3) + 4gr^3R_0^3}{8(RR_0)^3} + \frac{r^6(R^5 - R_0^5) + 6gr^5R_0^5}{16(RR_0)^5} + \dots$$

If we let g go to zero, then the expression becomes the difference in sag between two spheres of different radius (R and R_0), which isn't interesting, and is an old result. On the other hand, if we set $R = R_0$ we get the sag between the lathe-turned part and a reference sphere of the same radius, which has a very simple and revealing form:

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$$\Delta z = g \left[\left(\frac{r}{R} \right) + \frac{1}{2} \left(\frac{r}{R} \right)^3 + \frac{3}{8} \left(\frac{r}{R} \right)^5 + \dots \right]$$

The sag is proportional to the offset g , and is expressed solely in terms of the odd powers of (r/R) . To lowest order, the error is a conical error gr/R . This is not surprising – the tip of that gothic window or that dimple is simply a small cone. This is, at least for small values of r , the leading term. As we go further from the axis, of course, the higher odd terms will dominate.

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How do we express that conical term in our present system. We have been expressing the departure from the spherical reference in terms of polynomials in **x** and **y** (or, alternatively, as Zernike polynomials). We express these in the general form:

$$\Delta z = \sum_{n,m} a_{nm} x^n y^m$$

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But our present expression is in terms of $\mathbf{r} = (\mathbf{x}^2 + \mathbf{y}^2)^{1/2}$, which *cannot* be expressed as a sum of powers of **x** and **y**. It is true that if you restrict yourself to values very near the x-axis you can approximate **r** in powers of **x** and **y**. (In fact, this is true if you restrict yourself to any line with a well-defined relationship between **x** and **y**), but that is not our case – we consider spot shifts and surface fitting over a large region, including a very large area that is nowhere near the **x**- axis.

What we want is an approach that uses our current setup and software for a quick and simple solution. What if we were to use our present system to map the variation in sag from that of a target sphere as a function of radius in terms of the even powers we can use (since we can't use odd powers of radius). The simplest way to do this is the most direct. It will be described below in detail.

At any position in the vicinity of the Center of Curvature position (CoC) our knowledge of the reference sphere radius (which is equal to the distance we are at from the Surface position) enables us to translate the surface deviation **h(x,y)** into the true surface shape by simply adding the reference sphere sag (given by $\mathbf{R}_{\text{Ref}}(1 - (\mathbf{r}/\mathbf{R}_{\text{Ref}})^2)^{1/2}$), where \mathbf{R}_{Ref} is the reference sphere radius and $\mathbf{r} = (\mathbf{x}^2 + \mathbf{y}^2)^{1/2}$). We simply perform a least-square fit of this true surface shape to that of an off-centerlathed piece, using as our variables the offset **g** and the true radius of curvature of the surface **R_{True}**. If the user can supply **R_{True}**, so much the better – the search for the minimum of Chi Squared becomes a one-dimensional search.

In other words, the software searches for the value of **g** (and, if necessary, **R_{True}**) that minimizes the expression:

$$X^2 = \sum \left\{ Sag(x_i, y_j, R_{Ref}) + h(x_i, y_j, R_{Ref}) - f(x_i, y_j, R_{True}, g) \right\}^2$$

Where:

$$Sag(x_i, y_j, R_{Ref}) = R_{Ref} \left[1 - \sqrt{1 - \left(\frac{x_i^2 + y_j^2}{R_{Ref}^2} \right)} \right]$$

$$h(x_i, y_j, R_{Ref}) = \sum_{n,m} a_{nm} (R_{Ref}) x_i^n y_j^m$$

$$f(x_i, y_j, g, R_{True}) = R_{True} \left[1 - \sqrt{1 - \frac{\left(\sqrt{x_i^2 + y_j^2} - g \right)^2}{R_{True}^2}} \right]$$

The equations are not linear, so the minimization cannot be performed using matrix methods. The program must perform a regular search for the minimum of the chi squared function, using one of the many methods available.

This formulation assumes that the part is properly aligned and centered. This method can be modified to accommodate decentered and tilted parts, but it would be easier if the parts were properly positioned.

Once the coefficients describing the surface have been obtained using the above formulas they can be used to construct an accurate three-dimensional map of the surface from which any desired quantity can be derived. This includes, but is not limited to, determination of the radius of curvature of a spherical part, determination of the shape factor of an aspheric part, determination of the toric parameters of a toric

part, determining radius of curvature along selected meridians of a part, determining aspheric coefficients along selected meridians of a part, determining the "best fit" sphere, parabola, hyperbola, or other defined form to the surface. It can be used to determine lateral offset and tilt of a preselected form. It can be used to determine if an offset exists between a programmed lathe tool and the lathe axis by measuring the parameters of the fit. Knowledge of the surface profile as determined by the device combined with mathematical models for the expected shapes allow many determinations of desired measurements by those skilled in the art.

The foregoing algorithms for extracting surface and other information from the measured deviated spot locations can be readily programmed in a variety of program languages along with providing the graphical, tabular, and other data values. Fig. 10 shows, for example, one screen interface that shows a three-dimensional surfaced map along with various dialog boxes that provide the user with the ability to select options, operations, part description, and display types.

Figs. 11A-D and 12A-D show contour and three-dimensional maps of a surface as a function of defocus position, Figs. 13 and 14 are output screens illustrating coefficient plots versus position of the wavefront origin with respect to a test surface for a toric and sphere, respectively, and Fig. 15 shows one possible format for displaying toric and/or spherical information.

One possible general flow chart consistent with the inventive method is given by the following:

Input the type of measurement desired:

- a.) Generate Surface Profile only
- b.) Measure Radius of Curvature of Spherical Part
- c.) Measure Spherical Radius of Curvature, Cylindrical Radius of Curvature, and Angle for Toric Part
- d.) Measure Shape Factor or Conic Constant of Aspheric Part
- e.) Measure Aspheric Coefficients for Aspheric Part
- f.) Other

- 1.) Input Target Radius, if known, or indicate that Radius is unknown. Input other data (toric angle, etc.) if relevant.
- 2.) Perform measurement of spot deviation in the vicinity of the Surface location (i.e., with the translation stage positioned so that the focal point of the objective lies near the surface of the part under test. Locate the position at which the spot locations differ from the reference positions by at most a linear shift. Designate this the “zero” position for the stage, and refer all other positions to this one. If no “surface” location can be found produce an “error” message. This indicates that the surface finish of the part is too poor for measurement, or that the surface at the center is tilted too far from normal to the optical axis, or that no part is present.
- 3.) Go to the vicinity about one radius of curvature from this location. If the radius is not known, search for the location at which one again finds a disposition of spots similar to that found at the reference location or at the Surface position. If no such position can be found, report this in an “error” message. It indicates that the radius of curvature of the part exceeds the range of the machine, or else the finish of the part is too poor to allow measurement or there is no part or there is extreme misalignment.
- 4.) Perform at least one measurement but preferably a series of measurements at the “Center of Curvature” (CoC) location, similar to that performed near the “Surface” location. Measurements are preferably performed at several locations in the vicinity of the CoC. At each position the shifts in the spot locations are measured. From these shifts and the known distance z from the surface (and the known parameters of the SMI device) the coefficients a_{10} , a_{01} , etc. of the polynomial describing the deviation of the surface from a reference sphere of radius z are determined.
- 5.) Surface maps of the surface deviation at selected positions are generated and displayed.
- 6.) If a specific Measurement has been requested the software uses the relevant formulae to calculate the needed quantities from the positions z and the

coefficients $a_{nm}(z)$. For spherical parts the Radius of Curvature can be calculated. For Toric parts the two Radii of Curvature and the angles the axes of the radii make with the reference axis of the SMI are calculated. For Conic Section parts the Conic Constant or Shape Factor is calculated (as well as the base Radius of Curvature). Other measurements may be added to this list. Least square algorithms can be applied to fit predetermined analytical functions, spheres, aspheres, torics, or the like, to the measured surface or wavefront shape.

Those skilled in the art will be able to imagine other variants based on the teaching of the disclosure. Some of those variants are shown in Figs. 16 through 21.

Fig. 16 is a diagrammatic elevational view similar to Fig. 5 with the addition of a stationary positive lens 82 located forward of the microscope objective 70 to enable measurement of long radius parts where parts from Fig. 5 that reappear here in Fig. 16 bear the same numerical identification they had in Fig. 5. If lens 82 has a focal length, f_2 , then the radius of a part as indicated at 84 is given by:

$$R = f_2^2 / x$$

where x is the displacement of the microscope objective 70 required for collimation off of the reflective part 84. If x is positive, then R is convex, and if x is negative, then R is concave.

Reference is now made to Fig. 17 which shows a diagrammatic elevational view of an embodiment of the invention that is similar to Fig. 5 except for the absence of the objective which has been removed to enable measurement of flat surfaces that are at least partially reflective. With the objective removed, a flat object such as that designated at 86 can be tested for the flatness of its partially reflective surface by causing it to be illuminated with a plane wavefront 75 that now becomes the reference against which any wavefront distortion caused by the test surface may be compared as before. Again, repeated parts are identified here with their previous number.

Fig. 18 is a diagrammatic elevational view similar to Fig. 17 except for the presence of an additional mirror and a relay system for measuring the wavefront error of transmissive filters over their bandpass. As can be seen here, a relay system comprising lenses 88 and 90 is placed in the intervening space between beamsplitter 80 and a bandpass filter 92. Plane reference wavefront 75 passes through bandpass filter 92 after which it impinges on flat mirror 94 from which it reflects to travel back through bandpass filter 92, now having made a double pass through it, enters the relay system, and emerges as a more or less distorted wavefront which enters the camera 76. Because the filter transmits only the light within its bandpass, this embodiment measures the wavefront error of the filter only within that bandpass. Thus, the use of a broadband source instead of a spectrally narrow source has the advantage of being able to test filters whose bandpasses can span a broad spectral range.

Fig. 19 is a diagrammatic elevational view of an embodiment of the invention similar to that shown in Fig. 17 with the addition of a beam expansion section to measure large flat surfaces. The beam expansion section comprises two positive lenses 96 and 98 that operate in conjunction with one another to enlarge the diameter of the plane reference wavefront so that it can cover a larger area of a reflective part to be measured as, for example, the flat designated at 99. Alternative telescope geometries can also be used.

Fig. 20 is a diagrammatic elevational view of an embodiment of the invention similar to that of Fig. 18 except for the absence of a relay section and, like the embodiment of Fig. 18 measures the wavefront error of transmissive filters over their bandpass. This embodiment is suitable for use where a relay section is not needed to image the part under test on to the lenslet array.

Reference is now made to Fig. 21 which is a diagrammatic elevational view of an alternative embodiment of the invention that uses an intervening telescope between the objective and CCD array to make full use of the available numerical aperture (NA) of the objective. Here, there is an objective 100, a CCD array 102, and crossed lenticular lens 104, all of which operate as before. The optical path between objective 100 and CCD 102 includes an intervening telescope comprising lenses 110 and 112

and a pair of mirrors 106 and 108 for folding it for vertical compactness. The purpose of the telescopic lenses 110 and 112 is to optically scale the size of the CCD and lenticular array so that they fill the pupil of objective 100 to make full use of its numerical aperture (NA). As a convenience, a light source 116 is introduced in the telescope via beamsplitter 114 that is conjugate to a spatial filter 120 that operates to eliminate stray light.

Thus, it will be appreciated that spot sizes, CCD resolution, pixel saturation levels, objective NA and magnification, and pinhole size are among design parameters that may be varied. In addition, it will be appreciated that scaling optics may be placed between the microscope objective and the lenticular screen or the image plane of the lenticular array and the CCD to reimage the array of spots onto the CCD to rescale the relative sizes of the spots with respect to the pixels. Trigonometric polynomials or other series approximations for surface shape may be used. It will also be appreciated that the thickness and power of an element may be derived by examining both front and rear surfaces. In addition, the use of a strobe light or pulsed source may be used in place of a continuous source to study the dynamic properties of surfaces and transmitting components and the apparatus and test samples may be moved relative to one another to scan the properties of the surface in, for example, a web or scanning process. It will also be clear that the two-dimensional CCD array may be replaced by a one-dimensional array that scans across the focal plane of the crossed lenticular screen array or its equivalent. Accordingly, it is intended that these and other modifications and variations be within the scope of the invention.

CLAIMS:

- 1 1. Apparatus for automatically measuring the surface properties of optical
2 elements, said apparatus comprising:
3 a support for an element having at least one test surface to be measured;
4 means for generating an output beam having a predetermined wavefront
5 profile;
6 means for controllably positioning said output beam with respect to said
7 support so that said predetermined wavefront profile thereof impinges on said element
8 from a predetermined direction and then is reflected to travel opposite said
9 predetermined direction as a distorted wavefront containing distortions that vary in
10 accordance with the topography of said test surface and the position of said output
11 beam; and
12 means for sampling said distorted wavefront profile at predetermined locations
13 thereover as said output beam is moved relative to said test surface and determining
14 the local deformation of said wavefront everywhere corresponding to a sampled
15 location and the position of said output beam with respect to said test surface.
- 1 2. The apparatus of claim 1 further including analytical means for representing
2 the topography of said test surface with a mathematical approximation comprising a
3 series of coefficients and variables; calculating the value of said coefficients based on
4 the local deformation of said wavefront at at least one position of said source with
5 respect to said test surface.
- 1 3. The apparatus of claim 2 wherein said analytical means includes means for
2 performing an optimization analysis using the values of said coefficients calculated for
3 each position of said source and test surface to arrive at a final value for said
4 coefficients that are used for said mathematical approximation to represent the shape
5 of said surface to a predetermined accuracy.

4. The apparatus of claim 1 wherein said predetermined wavefront comprises a plane wavefront.

5. The apparatus of claim 1 wherein said predetermined wavefront comprises a nominally spherical wavefront.

6. The apparatus of claim 1 wherein said means for generating said output beam comprises a light source and collimating optics.

7. The apparatus of claim 6 further including a well-corrected objective lens.

8. The apparatus of claim 1 further including a positive lens located in a fixed position with respect to said support and along said predetermined direction to facilitate the measurement of parts having long radii of curvature.

9. The apparatus of claim 4 further including a reflective means positioned with respect to said support to facilitate the measurement of transmitted wavefront errors in optical bandpass components including filters and windows.

10. The apparatus of claim 9 further including a relay section.

11. The apparatus of claim 4 further including a beam expansion section.

12. The apparatus of claim 1 wherein said means for sampling said distorted wavefront comprises a two-dimensional lens array and a two-dimensional photodetector array having discrete sensing elements.

13. The apparatus of claim 12 wherein said two-dimensional lens array comprises a pair of crossed lenticular screens with index mismatching material between them.

14. The apparatus of claim 12 wherein said means for generating said output beam comprises a microscope objective lens and further including a telescopic section between said microscope objective lens and said two-dimensional lens array to image said two-dimensional photodetector array into the pupil of said microscope objective lens.

15. Apparatus for automatically measuring the properties of surfaces that are at least partially specularly reflective, said apparatus comprising:

a support for an element having at least one test surface to be measured;

a source having an output with a predetermined wavefront profile;

means for controllably moving said source and said support relative to one another so that a test surface in said support continuously reflects said output from said source back towards said source while distorting said wavefront profile thereof in accordance with the topography of said test surface and the relative position of said source with respect to said test surface; and

means for sampling said distorted wavefront profile at predetermined locations thereover as said source is moved relative to said test surface and determining the local deformation of said wavefront everywhere corresponding to a sampled location and the position of said source with respect to said test surface.

16. The apparatus of claim 15 further including analytical means for representing the topography of said test surface with a mathematical approximation comprising a series of coefficients and variables; calculating the value of said coefficients based on the local deformation of said wavefront at at least one position of said source with respect to said test surface.

17. The apparatus of claim 15 wherein said analytical means includes means for performing an optimization analysis using the values of said coefficients calculated for each position of said source and test surface to arrive at a final value for said

4 coefficients that are used for said mathematical approximation to represent the shape
5 of said surface to a predetermined accuracy.

1 18. The apparatus of claim 1 wherein said means for sampling said distorted
2 wavefront profile comprises a two-dimensional lenslet array having a focal plane and a
3 one-dimensional photodetector array arranged to scan across said focal plane.

1 19. The apparatus of claim 1 wherein said means for generating an output
2 beam comprises one of a pulsed light source or strobe.

1 20. A method for automatically measuring the surface properties of optical
2 elements, said method comprising the steps of:
3 supporting an element having at least one test surface to be measured;
4 generating an output beam having a predetermined wavefront profile;
5 controllably positioning said output beam with respect to said support so that
6 said predetermined wavefront profile thereof impinges on said element from a
7 predetermined direction and then is reflected to travel opposite said predetermined
8 direction as a distorted wavefront containing distortions that vary in accordance with
9 the topography of said test surface and the position of said output beam; and
10 sampling said distorted wavefront profile at predetermined locations thereover
11 as said output beam is moved relative to said test surface and determining the local
12 deformation of said wavefront everywhere corresponding to a sampled location and the
13 position of said output beam with respect to said test surface.

1 21. The method of claim 20 further including the step of analytically
2 representing the topography of said test surface with a mathematical approximation
3 comprising a series of coefficients and variables and calculating the value of said
4 coefficients based on the local deformation of said wavefront at at least one position of
5 said source with respect to said test surface.

1 22. The method of claim 21 wherein said coefficients are polynomial of at
2 least second order.

23. The method of claim 22 further including the step of determining the shape
factor of an aspheric surface.

1 24. The method of claim 21 further including the step of determining the offset
2 between axis of the surface being measured and that of the apparatus used to measure
3 it.

1 25. The method of claim 21 further including the step of determining any
2 offset between a programmed lathe tool and the axis of the lathe.

ABSTRACT OF THE DISCLOSURE

An automated apparatus and method for measuring properties of optical components based on wavefront sensing and analysis. A wavefront of predetermined profile is directed at a surface to be measured so that it is more or less distorted in accordance with the shape of the surface and the distorted wavefront is sensed and analyzed. From the information derived from the distorted wavefront and other knowledge of the relationship between the surface and position of the wavefront of predetermined profile, the shape of the surface may be inferred along with other properties such as radius of curvature, focal length, conic constants, asphericity, toricity, tilt, and decentering. Concave, convex, cylindrical, and flat parts may be measured along with wavefront errors in bandpass transmitting components such as lenses, filters, and windows.

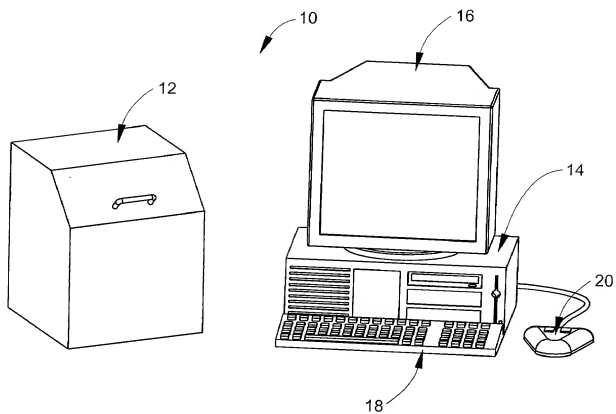


FIG. 1

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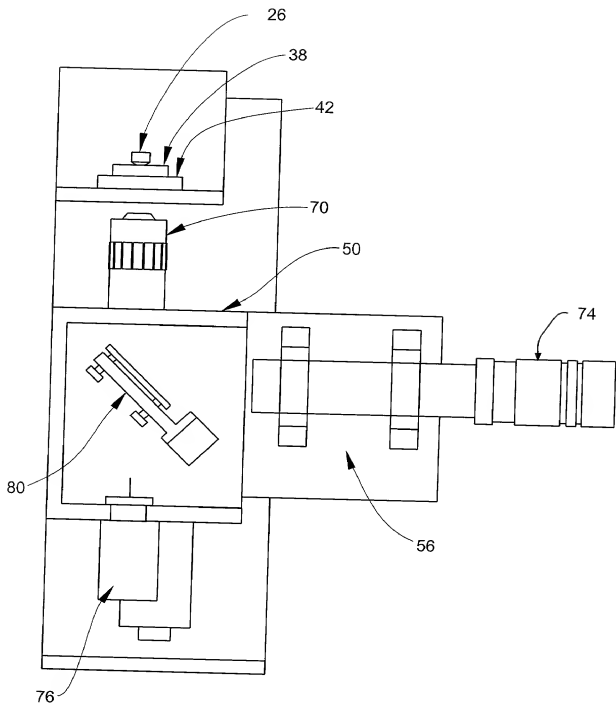


FIG. 2

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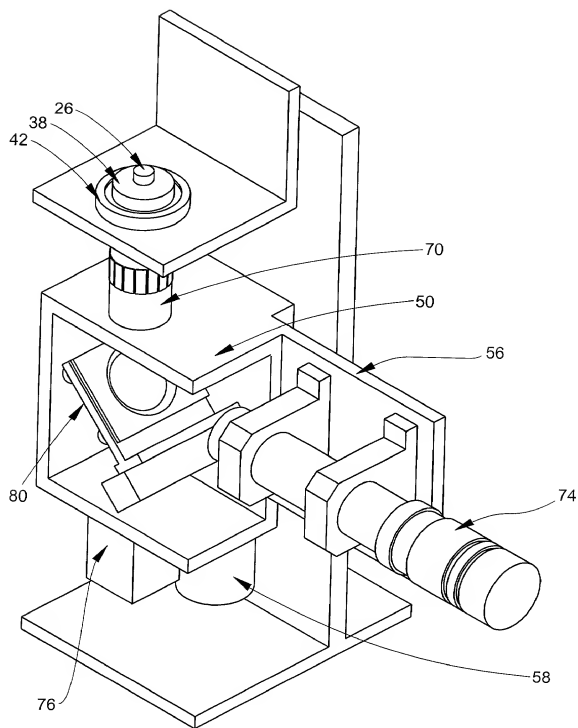


FIG. 3

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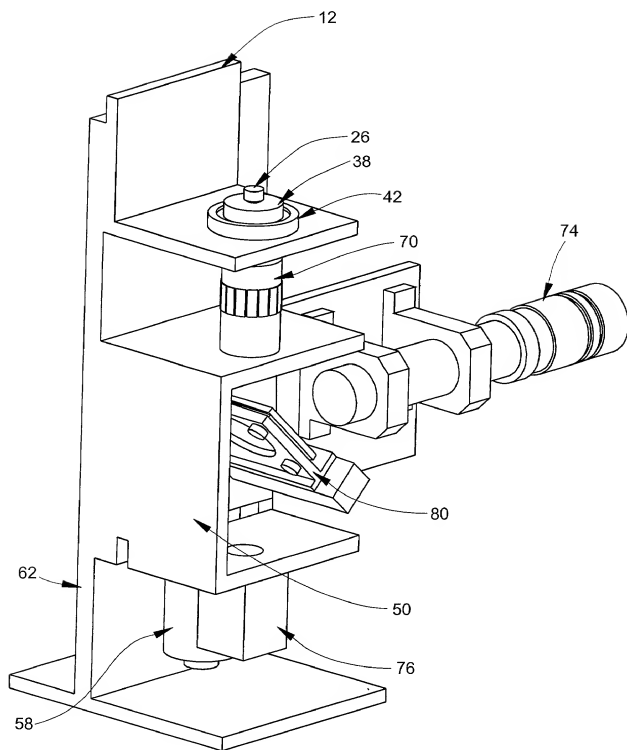


FIG. 4

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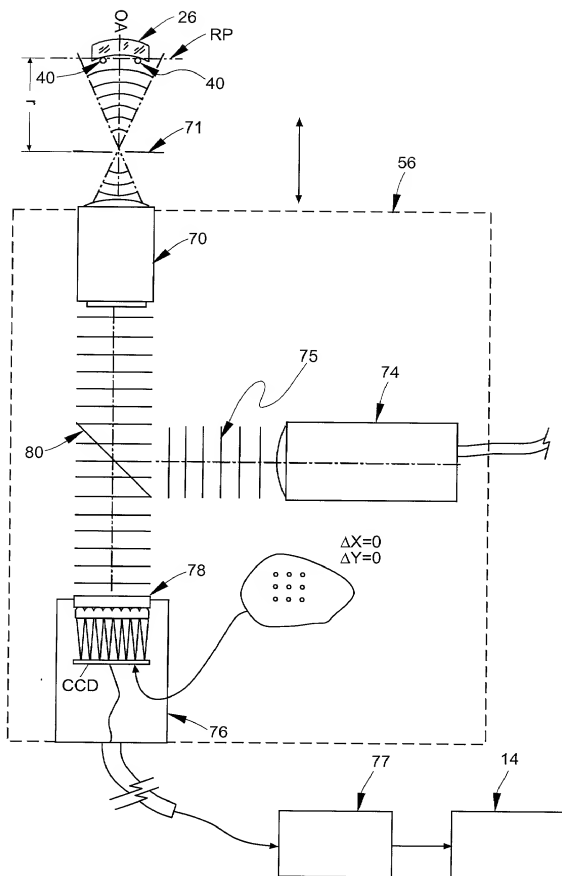


FIG. 5

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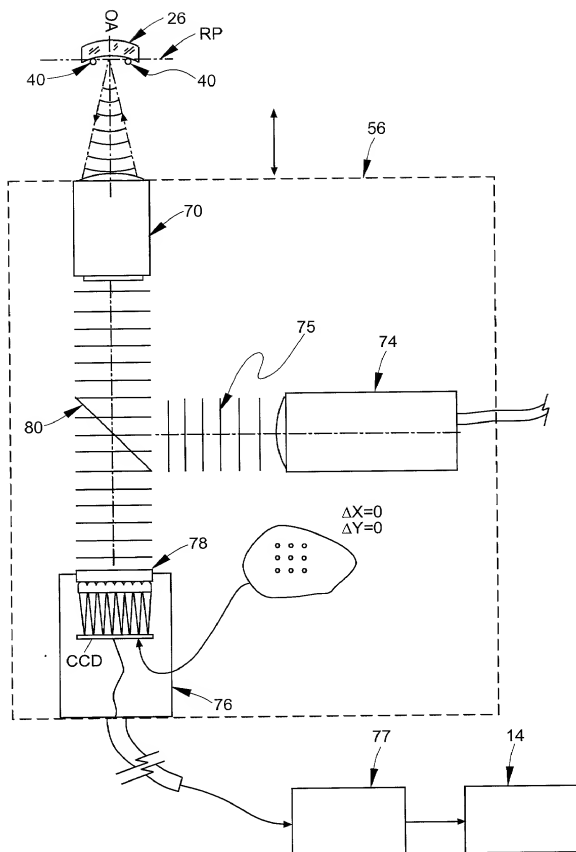
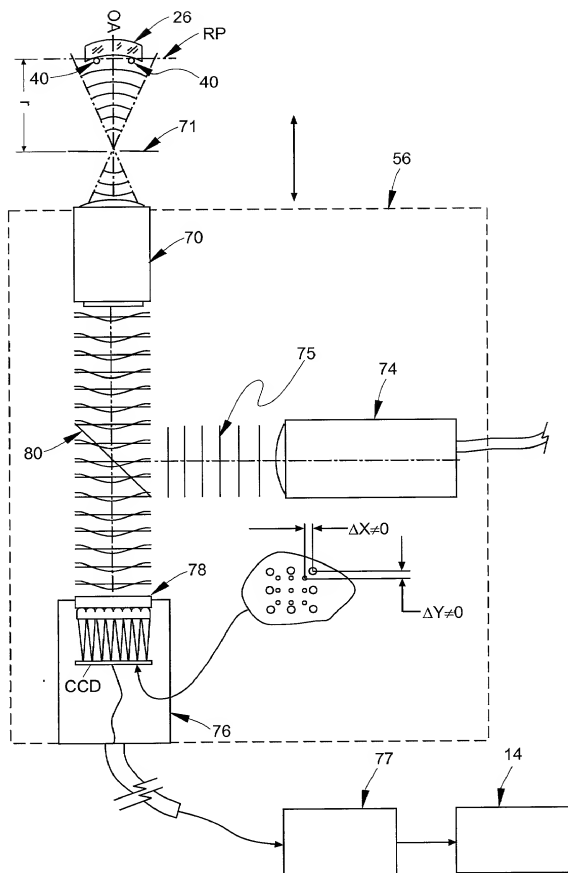


FIG. 6

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002007" 6/29/1953

<p>THRESHOLD ADJUSTMENT</p> <p>THRESHOLD 255 <input type="text" value="38"/> <input type="button" value="0"/></p>		<p>PEAK LOCATION SEARCH PEAKS</p> <p>PEAK <input type="text"/> CENTROID <input type="text"/></p> <p>REFERENCE ADJUSTMENT <input type="text"/></p> <p>REFERENCE <input type="text"/> LABEL <input type="text"/></p>		<p>DRAWING</p> <p>TRACES <input type="button" value="REDRAW"/></p> <p>SAVE AS BASE COORDINATES <input type="button" value="SAVE"/></p>		<p>DISPLAY CALCULATION</p> <p>CALCULATE SHIFT <input type="button" value="POSITIVE SLOPE"/></p>	

FIG. 8

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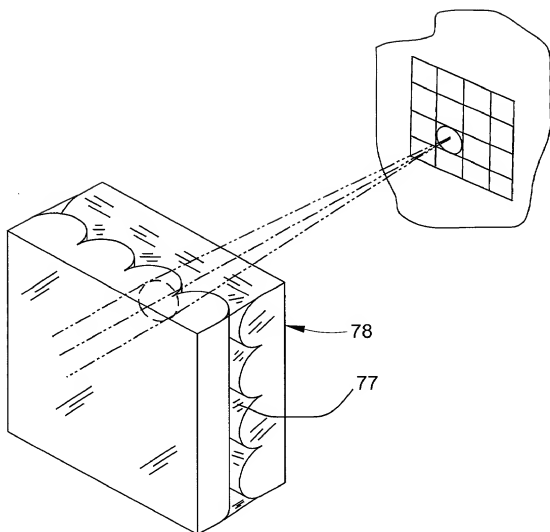


FIG. 9

UNIT UNDER TEST

☐ CONCAVE☒ CONVEX

EXPECTED RADIUS

8 mm

FOCAL LENGTH

20 mm

CALCULATED RESULTS

RADIUS 8.00159 mm

MOTION CONTROL

MOTOR...

FRAME GRABBER
CONTROL

ACTIVE IMAGE

DISPLAY TYPES

☒ MESH☒ SHADED☐ CONTOURS☒ ZONES

OPTIONS

☒ TURN OFF LINEAR TERM☒ TURN OFF FOURTH TERM☒ MOVE OFFSET☐ TURN OFF SECOND TERM☐ DATA FILTERING☐ SHOW RESULTS☐ TURN OFF THIRD TERM☐ DEFOCUS POSITIVE☐ SUBTRACT RESIDUAL

OPERATIONS

LOCATE FOCUS

LOCATE RADIUS

MEASUREMENT

SURFACE CONTOURS

MAPPING ORDER

10/22

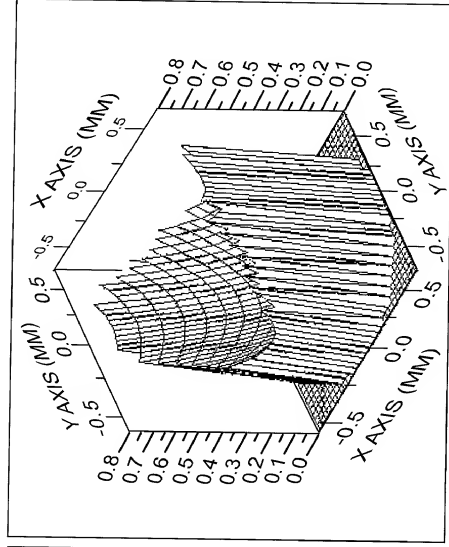


FIG. 10

MAPPING AT DEFOCUS 0 MICRONS
PEAK TO VALLEY VALUE: 0.516 MICRONS
RMS VALUE: 0.113414 MICRONS

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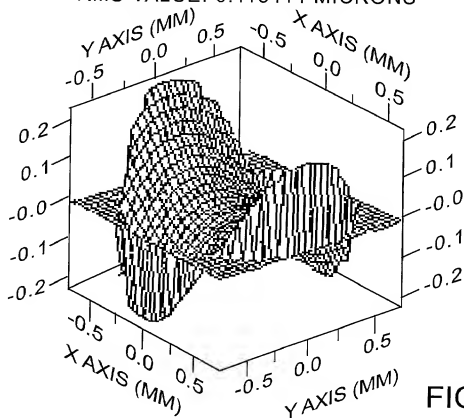


FIG. 11A

MAPPING AT DEFOCUS 100 MICRONS
PEAK TO VALLEY VALUE: 0.500 MICRONS
RMS VALUE: 0.212682 MICRONS

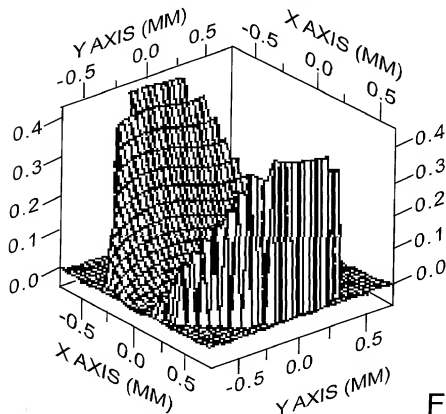


FIG. 11B

MAPPING AT DEFOCUS 200 MICRONS
PEAK TO VALLEY VALUE: 0.677 MICRONS
RMS VALUE: 0.366139 MICRONS

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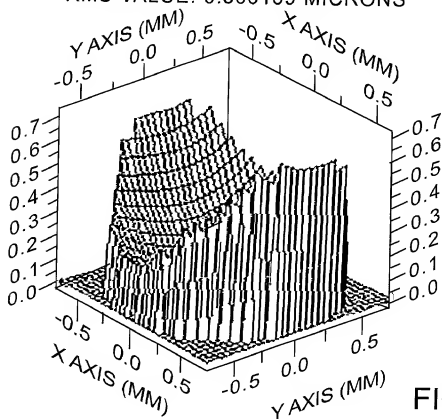


FIG. 11C

MAPPING AT DEFOCUS 300 MICRONS
PEAK TO VALLEY VALUE: 0.835 MICRONS
RMS VALUE: 0.515124 MICRONS

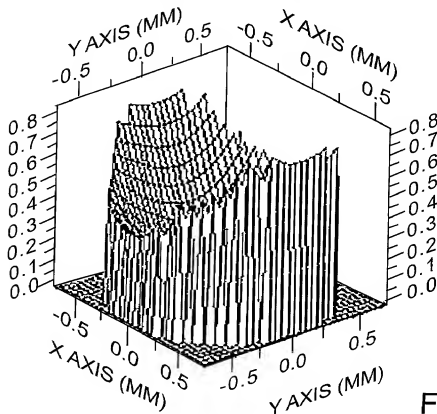


FIG. 11D

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MAPPING AT DEFOCUS 0 MICRONS
PEAK TO VALLEY VALUE: 0.611 MICRONS
RMS VALUE: 0.133521 MICRONS

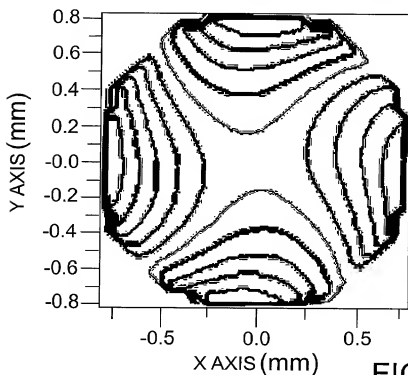


FIG. 12A

MAPPING AT DEFOCUS 100 MICRONS
PEAK TO VALLEY VALUE: 0.565 MICRONS
RMS VALUE: 0.238394 MICRONS

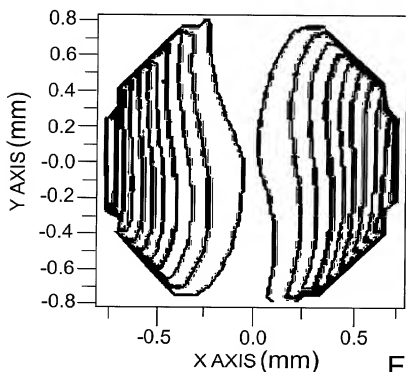


FIG. 12B

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MAPPING AT DEFOCUS 200 MICRONS
PEAK TO VALLEY VALUE: 0.722 MICRONS
RMS VALUE: 0.389452 MICRONS

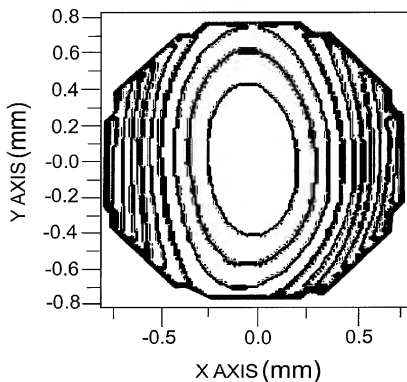


FIG. 12C

MAPPING AT DEFOCUS 300 MICRONS
PEAK TO VALLEY VALUE: 0.835 MICRONS
RMS VALUE: 0.515124 MICRONS

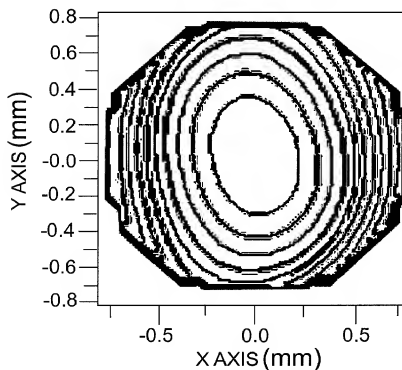


FIG. 12D

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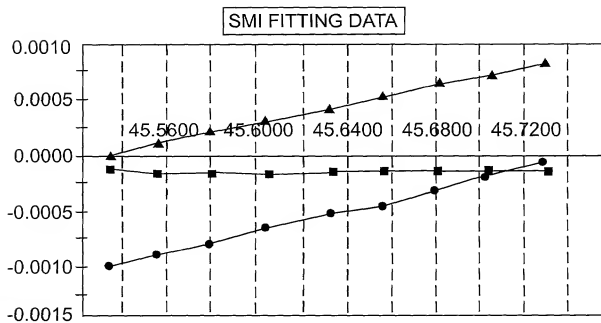


FIG. 13

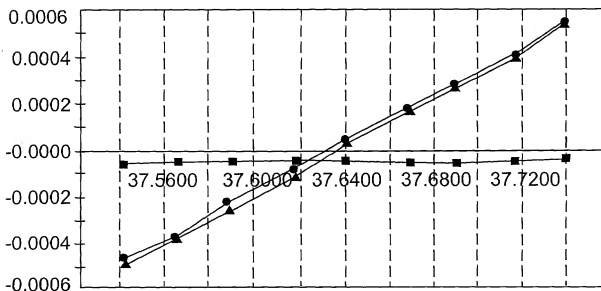


FIG. 14

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EXPECTED VALUE	MEASURED VALUES
MEAN RADIUS <input type="text" value="8"/> mm	MEAN RADIUS <input type="text" value="8.00623"/> mm
	SPHERICAL RADIUS <input type="text" value="7.94381"/> mm
	CYLINDRICAL RADIUS <input type="text" value="8.06864"/> mm
	AXIS <input type="text" value="85.5778"/> DEG

FIG. 15

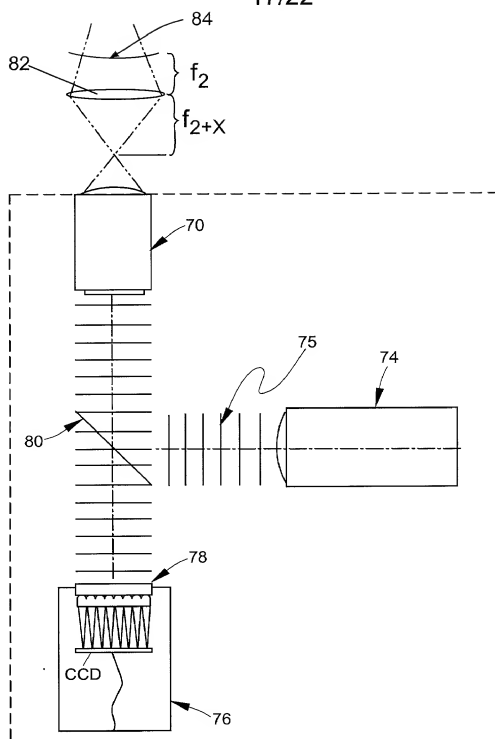


FIG. 16

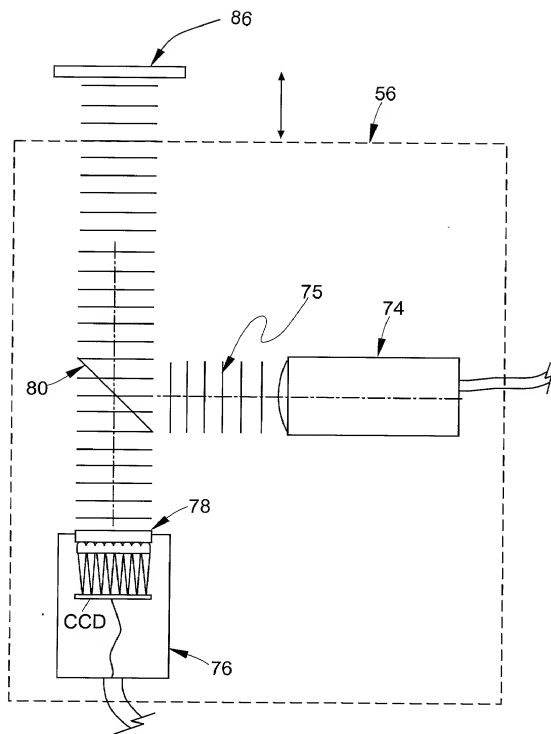


FIG. 17

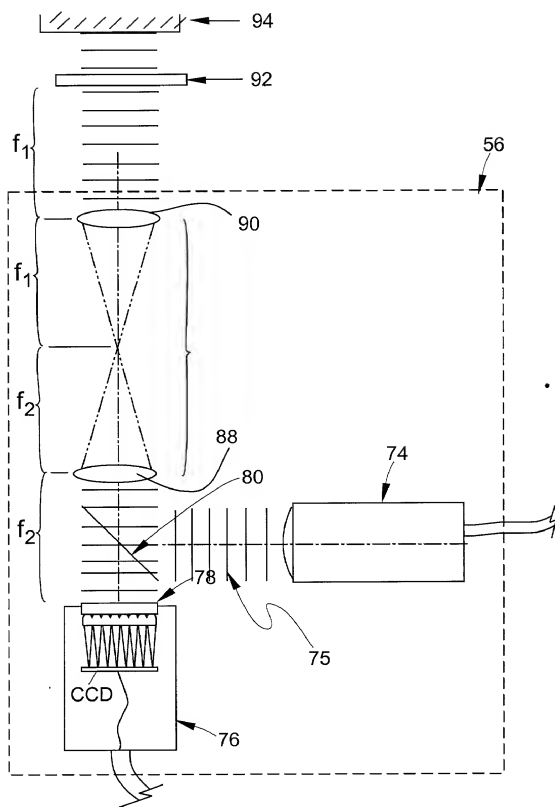


FIG. 18

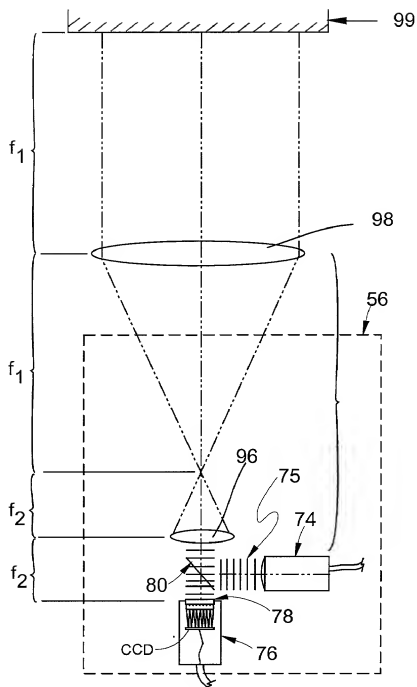


FIG. 19

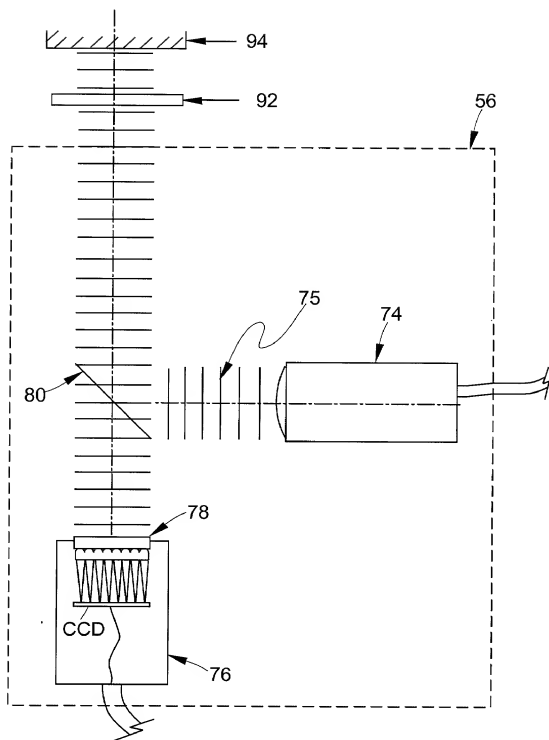


FIG. 20

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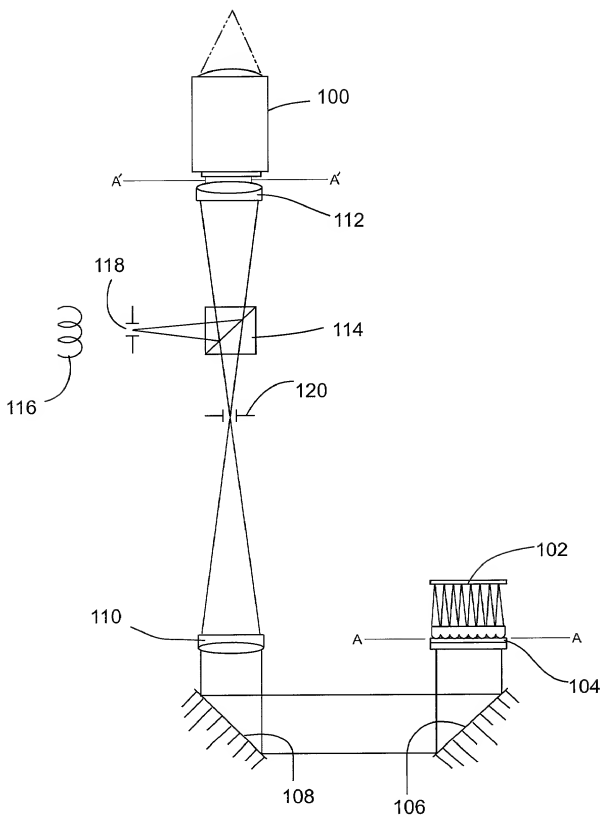


FIG. 21

002001" 6-9/2/960

Docket No.
0205/US

Declaration and Power of Attorney For Patent Application

English Language Declaration

As a below named inventor, I hereby declare that:

My residence, post office address and citizenship are as stated below next to my name,

I believe I am the original, first and sole inventor (if only one name is listed below) or an original, first and joint inventor (if plural names are listed below) of the subject matter which is claimed and for which a patent is sought on the invention entitled

AUTOMATED OPTICAL MEASUREMENT APPARATUS AND METHOD

the specification of which

(check one)

☒ is attached hereto.

☐ was filed on _____ as United States Application No. or PCT International Application Number _____ and was amended on _____ (if applicable)

I hereby state that I have reviewed and understand the contents of the above identified specification, including the claims, as amended by any amendment referred to above.

I acknowledge the duty to disclose to the United States Patent and Trademark Office all information known to me to be material to patentability as defined in Title 37, Code of Federal Regulations, Section 1.56.

I hereby claim foreign priority benefits under Title 35, United States Code, Section 119(a)-(d) or Section 365(b) of any foreign application(s) for patent or inventor's certificate, or Section 365(a) of any PCT International application which designated at least one country other than the United States, listed below and have also identified below, by checking the box, any foreign application for patent or inventor's certificate or PCT International application having a filing date before that of the application on which priority is claimed.

Prior Foreign Application(s)

Priority Not Claimed

(Number)

(Country)

(Day/Month/Year Filed)

☐

(Number)

(Country)

(Day/Month/Year Filed)

☐

(Number)

(Country)

(Day/Month/Year Filed)

☐

60/160,949	Oct. 22, 1999
(Application Serial No.)	(Filing Date)

(Application Serial No.) _____ (Filing Date) _____

(Application Serial No.) _____ (Filing Date) _____

I hereby claim the benefit under 35 U. S. C. Section 120 of any United States application(s), or Section 365(c) of any PCT International application designating the United States, listed below and, insofar as the subject matter of each of the claims of this application is not disclosed in the prior United States or PCT International application in the manner provided by the first paragraph of 35 U.S.C. Section 112, I acknowledge the duty to disclose to the United States Patent and Trademark Office all information known to me to be material to patentability as defined in Title 37, C. F. R., Section 1.56 which became available between the filing date of the prior application and the national or PCT International filing date of this application:

<u>09/328,972</u>	<u>JUN 9, 1999</u>	<u>Pending</u>
(Application Serial No.)	(Filing Date)	(Status) (patented, pending, abandoned)

(Application Serial No.)	(Filing Date)	(Status) (patented, pending, abandoned)
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(Application Serial No.)	(Filing Date)	(Status) (patented, pending, abandoned)

I hereby declare that all statements made herein of my own knowledge are true and that all statements made on information and belief are believed to be true; and further that these statements were made with the knowledge that willful false statements and the like so made are punishable by fine or imprisonment, or both, under Section 1001 of Title 18 of the United States Code and that such willful false statements may jeopardize the validity of the application or any patent issued thereon.

POWER OF ATTORNEY: As a named inventor, I hereby appoint the following attorney(s) and/or agent(s) to prosecute this application and transact all business in the Patent and Trademark Office connected therewith. *(list name and registration number)*

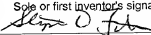
FRANCIS J. CAUFIELD REGISTRATION NO. 27,425

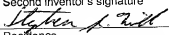
Send Correspondence to:


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LEXINGTON, MA 02421-7025


Direct Telephone Calls to: *(name and telephone number)*

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Citizenship US	
Post Office Address Same As Residence above	

Full name of fifth inventor, if any	
Fifth inventor's signature	Date
Residence	
Citizenship	
Post Office Address	

Full name of sixth inventor, if any	
Sixth inventor's signature	Date
Residence	
Citizenship	
Post Office Address	